Package 'hdMTD'

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Type Package

Title Inference for High-Dimensional Mixture Transition Distribution Models

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Description Estimates parameters in Mixture Transition Distribution (MTD) models, a class of high-order Markov chains. The set of relevant pasts (lags) is selected using either the Bayesian Information Criterion or the Forward Stepwise and Cut algorithms. Other model parameters (e.g. transition probabilities and oscillations) can be estimated via maximum likelihood estimation or the Expectation-Maximization algorithm. Additionally, 'hdMTD' includes a perfect sampling algorithm that generates samples of an MTD model from its invariant distribution. For theory, see Ost & Takahashi (2023) https://jmlr.org/papers/v24/22-0266.html.

URL https://github.com/MaiaraGripp/hdMTD

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as.MTD

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as.MTD

Coerce an EM fit to an MTD model

Description

Convenience coercion to rebuild an object of class "MTD" from an "MTDest" fit (or its summary). This simply feeds the estimated parameters back into MTDmodel.

Usage

```
as.MTD(x, ...)
```

Arguments

x An object of class "MTDest" or "summary.MTDest".

... Further arguments passed to or from other methods (ignored).

Value

An object of class "MTD" as returned by MTDmodel.

See Also

MTDest, MTDmodel

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Examples

```
## Not run:
 set.seed(1)
 MTD <- MTDmodel(Lambda = c(1, 3), A = c(0, 1), lam0 = 0.05) # generates MTD model
 X <- perfectSample(MTD, N = 400) # generates MTD sample
 init <- list(</pre>
   p0 = c(0.4, 0.6),
   lambdas = c(0.05, 0.45, 0.5),
   pj = list(
      matrix(c(0.2, 0.8, 0.45, 0.55), byrow = TRUE, ncol = 2),
      matrix(c(0.25, 0.75, 0.3, 0.7), byrow = TRUE, ncol = 2)
   )
 )
 fit <- MTDest(X, S = c(1, 3), init = init) # estimates parameters from sample
 m <- as.MTD(fit) # generates an MTD model from estimated parameters
 str(m, max.level = 1)
## End(Not run)
```

countsTab

Counts sequences of length d+1 in a sample

Description

Creates a tibble containing all unique sequences of length d+1 found in the sample, along with their absolute frequencies.

Usage

```
countsTab(X, d)
```

Arguments

d

X A numeric vector, a single-column data frame, or a list with a sample from a

Markov chain. The first element must be the most recent observation.

value of the most recent must be the most recent observation

A positive integer specifying the number of elements in each sequence, which will be d+1. Typically, d represents the chain order or serves as an upper limit

for it.

Details

The function generates a tibble with d+2 columns. In the first d+1 columns, each row displays a unique sequence of size d+1 observed in the sample. The last column, called Nxa, contains the number of times each of these sequences appeared in the sample.

The number of rows in the output varies between 1 and $|A|^{d+1}$, where |A| is the number of unique states in X, since it depends on the number of unique sequences that appear in the sample.

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Value

A tibble with all observed sequences of length d+1 and their absolute frequencies.

Examples

```
countsTab(c(1,2,2,1,2,1,1,2,1,2), d = 3)
# Using simulated data.
set.seed(1)
M \leftarrow MTDmodel(Lambda = c(1, 3), A = c(1, 2), lam0 = 0.05)
X \leftarrow perfectSample(M, N = 400)
countsTab(X, d = 2)
```

 ${\rm dTV_sample}$

The total variation distance between distributions

Description

Calculates the total variation distance between distributions conditioned in a given past sequence.

Usage

```
dTV_sample(S, j, A = NULL, base, lenA = NULL, A_pairs = NULL, x_S)
```

Arguments

S	A numeric vector of positive integers (or NULL) representing a set of past lags. The distributions from which this function will calculate the total variation distance are conditioned on a fixed sequence indexed by S (the user must also input the sequence through the argument x_S).
j	A positive integer representing a lag in the <i>complement</i> of S. The symbols indexed by j vary along the state space A, altering the distribution through this single lag, and the size of this change is what this function seeks to measure.
A	A vector of unique nonnegative integers (state space) with at least two elements. A represents the state space. You may leave A=NULL (default) if you provide the function with the arguments lenA and A_pairs (see <i>Details</i> below).
base	A data frame with sequences of elements from A and their transition probabilities. base is meant to be an output from function $freqTab()$, and must be structured as such. The data frame must contain all required transitions conditioned on x_S (i.e. $length(A)^2$ rows with sequence x_S). See <i>Details</i> section for further information.
lenA	An integer >= 2, representing length(A). Required if A is not provided.

A two-column matrix with all unique pairs of elements from A. Required if A is A_pairs not provided.

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 x_S

A vector of length length(S) or NULL. If S==NULL, x_S will be set to NULL. x_S represents a sequence of symbols from A indexed by S. This sequence remains constant across the conditional distributions to be compared, representing the fixed configuration of the past.

Details

This function computes the total variation distance between distributions found in base, which is expected to be the output of the function freqTab(). Therefore, base must follow a specific structure (e.g., column names must match, and a column named qax_Sj, containing transition distributions, must be present). For more details on the output structure of freqTab(), refer to its documentation.

The total-variation distance is computed as

$$\frac{1}{2} \sum_{a \in \mathcal{A}} |\hat{p}(a|x_{-S}, x_{-j} = b) - \hat{p}(a|x_{-S}, x_{-j} = c)|,$$

for each pair of symbols b, c in A using the empirical conditional probabilities obtained from freqTab for the supplied S and j.

If you provide the state space A, the function calculates: lenA <- length(A) and A_pairs <- t(utils::combn(A, 2)). Alternatively, you can input lenA and A_pairs directly and let A <- NULL, which is useful in loops to improve efficiency.

Value

A single-row matrix with one column per pair of distinct elements from the state space A (so choose(length(A), 2) columns). Each entry corresponds to the total variation distance between a pair of distributions, conditioned on the same fixed past x_S (when S is not NULL), differing only in the symbol indexed by j, which varies across all distinct pairs of elements in A. When S is NULL, the row name is the empty string "".

```
set.seed(1)
M <- MTDmodel(Lambda = c(1, 4), A = c(1, 2, 3), lam0 = 0.1)
X <- perfectSample(M, N = 400)
ct <- countsTab(X, d = 5)

# --- Case 1: S non-empty
pbase <- freqTab(S = c(1, 4), j = 2, A = c(1, 2, 3), countsTab = ct)
dTV_sample(S = c(1, 2), j = 4, A = c(1, 2, 3), base = pbase, x_S = c(2, 3))
# --- Case 2: S = NULL
pbase2 <- freqTab(S = NULL, j = 1, A = c(1, 2, 3), countsTab = ct)
dTV_sample(S = NULL, j = 1, A = c(1, 2, 3), base = pbase2)</pre>
```

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Estimated transition probabilities

Description

Computes the Maximum Likelihood estimators (MLE) for an MTD Markov chain with relevant lag set S.

Usage

```
empirical_probs(X, S, matrixform = FALSE, A = NULL, warn = FALSE)
```

Arguments

X	A vector or single-column data frame containing a sample of a Markov chain $(X[1])$ is the most recent).
S	A numeric vector of unique positive integers. Typically, S represents a set of relevant lags.
matrixform	Logical. If TRUE, the output is formatted as a stochastic transition matrix.
A	A numeric vector of distinct integers representing the state space. If not provided, this function will set $A \leftarrow sort(unique(X))$.
warn	Logical. If TRUE, the function warns the user when the state space is automatically set as $A \leftarrow sort(unique(X))$.

Details

The probabilities are estimated as:

$$\hat{p}(a|x_S) = \frac{N(x_S a)}{N(x_S)}$$

where $N(x_S a)$ is the number of times the sequence x_S appeared in the sample followed by a, and $N(x_S)$ is the number of times x_S appeared (followed by any state). If $N(x_S) = 0$, the probability is set to 1/|A| (assuming a uniform distribution over A).

Value

A data frame or a matrix containing estimated transition probabilities:

- If matrixform = FALSE, the function returns a data frame with three columns:
 - The past sequence x_S (a concatenation of past states).
 - The current state a.
 - The estimated probability $\hat{p}(a|x_S)$.
- If matrixform = TRUE, the function returns a stochastic transition matrix, where rows correspond to past sequences x_S and columns correspond to states in A.

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Examples

```
# Simulate a chain from an MTD model
set.seed(1)
M <- MTDmodel(Lambda = c(1, 15, 30), A = c(1, 2, 3), lam0 = 0.05)
X <- perfectSample(M, N = 400)

# Estimate probabilities for different subsets S
empirical_probs(X, S = c(1, 30))
empirical_probs(X, S = c(1, 15, 30), matrixform = TRUE)</pre>
```

freqTab

A tibble containing sample sequence frequencies and estimated probabilities

Description

This function returns a tibble containing the sample sequences, their frequencies and the estimated transition probabilities.

Usage

```
freqTab(S, j = NULL, A, countsTab, complete = TRUE)
```

Arguments

S	A numeric vector of positive integers or NULL. Represents a set of past lags that must be present within the columns of the countsTab argument and are to be considered while estimating the transition probabilities. Both S and j cannot be NULL at the same time.
j	An integer or NULL. Typically represents a lag j in the <i>complement</i> of S. Both S and j cannot be NULL at the same time. See <i>Details</i> for further information.
A	A vector with nonnegative integers. Must have at least two different entries. A represents the state space.
countsTab	A tibble or a data frame with all sequences of length d+1 that appear in the sample, and their absolute frequency. This tibble is typically generated by the function countsTab(). If using a custom data frame not generated by countsTab(), make sure its format and column names match the expected structure; otherwise, errors may occur in freqTab().
complete	Logical. If TRUE all sequences that did not appear in the sample will be included

Details

The parameters S and j determine which columns of counts Tab are retained in the output. Specifying a lag j is optional. All lags can be specified via S, while leaving j = NULL (default). The output remains the same as when specifying S and j separately. The inclusion of j as a parameter improves clarity within the package's algorithms. Note that j cannot be an element of S.

in the output with frequency equal to 0.

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Value

A tibble where each row represents a sequence of elements from A. The initial columns display each sequence symbol separated into columns corresponding to their time indexes. The remaining columns show the sample frequencies of the sequences and the MLE (Maximum Likelihood Estimator) of the transition probabilities.

Examples

```
# Reproducible simulated data
set.seed(1)
M <- MTDmodel(Lambda = c(1, 4), A = c(1, 2, 3), lam0 = 0.1)
X <- perfectSample(M, N = 400)
ct <- countsTab(X, d = 5)

# Example with S non-empty and j specified
freqTab(S = c(1, 4), j = 2, A = c(1, 2, 3), countsTab = ct)

# Equivalent to calling with S = c(1,2,4) and j = NULL
freqTab(S = c(1, 2, 4), j = NULL, A = c(1, 2, 3), countsTab = ct)</pre>
```

hdMTD

Inference in MTD models

Description

This function estimates the relevant lag set in a Mixture Transition Distribution (MTD) model using one of the available methods. By default, it applies the Forward Stepwise ("FS") method, which is particularly useful in high-dimensional settings.

Usage

```
hdMTD(X, d, method = "FS", ...)
```

Arguments

X A vector or single-column data frame containing a chain sample.

d A positive integer representing an upper bound for the chain order.

method A character string indicating the method for estimating the relevant lag set. The

available methods are: "FS" (default), "FSC", "CUT", and "BIC". See the *Details* section and the documentation of the corresponding method functions for

more information.

Additional arguments for the selected method. If not specified, default values

will be used (see Details).

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Details

The available methods are:

• "FS" (Forward Stepwise): selects the lags by a criterion that depends on their oscillations.

- "CUT": a method that selects the relevant lag set based on a predefined threshold.
- "FSC" (Forward Stepwise and Cut): applies the "FS" method followed by the "CUT" method.
- "BIC": selects the lag set using the Bayesian Information Criterion.

The function dynamically calls the corresponding method function (e.g., hdMTD_FSC() for method = "FSC"). Additional parameters specific to each method can be provided via ..., and default values are used for unspecified parameters.

This function serves as a wrapper for the method-specific functions:

- hdMTD_FS(), for method = "FS"
- hdMTD_FSC(), for method = "FSC"
- hdMTD_CUT(), for method = "CUT"
- hdMTD_BIC(), for method = "BIC"

Any additional parameters (...) must match those accepted by the corresponding method function. If a parameter value is not explicitly provided, a default value is used. The main default parameters are:

- S = seq_len(d): Used in "BIC" or "CUT" methods.
- alpha = 0.05, mu = 1. Used in "CUT" or "FSC" methods.
- xi = 0.5. Used in "CUT", "FSC" or "BIC" methods.
- minl = 1, maxl = length(S), byl = FALSE. Used in "BIC" method. All default values are specified in the documentation of the method-specific functions.

BIC-specific notes. When method = "BIC", the object may carry additional BIC diagnostics:

- attr(x, "extras")\$BIC_out: exactly the object returned by hdMTD_BIC() (its type depends on BICvalue and byl: named numeric vector when BICvalue = TRUE; otherwise a character vector of labels, possibly including "smallest: <set>").
- attr(x, "BIC_selected_value"): when BICvalue = TRUE, the numeric BIC at the selected lag set (shown by summary()).

Value

An integer vector of class "hdMTD" (the selected lag set $S \subset \mathbb{N}^+$), with attributes:

- method, d, call, settings
- A: the state space actually used (either provided A, or sort(unique(X)) if A = NULL)
- (for method="BIC") extras: a list with BIC_out (exactly the object returned by hdMTD_BIC)
- (for method="BIC" and BICvalue = TRUE) BIC_selected_value: numeric BIC at the selected set

The returned object supports print() and summary() methods.

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See Also

```
hdMTD_FS, hdMTD_FSC, hdMTD_CUT, hdMTD_BIC, S, lags
```

Examples

```
# Simulate a chain from an MTD model
set.seed(1)
M <- MTDmodel(Lambda = c(1, 4), A = c(1, 3), lam0 = 0.05)
X <- perfectSample(M, N = 400)

# Fit using Forward Stepwise (FS)
S_fs <- hdMTD(X = X, d = 5, method = "FS", l = 2)
print(S_fs)
summary(S_fs)  # shows A used if A = NULL in the call

# Fit using Bayesian Information Criterion (BIC)
hdMTD(X = X, d = 5, method = "BIC", xi = 0.6, minl = 3, maxl = 3)</pre>
```

hdMTD-methods

Methods for objects of class "hdMTD"

Description

Printing and summarizing methods for lag-selection results returned by hdMTD.

Arguments

X	An object of class "hdMTD" or "summary.hdMTD", depending on the method.
object	An object of class "hdMTD".
settings	Logical (summary.hdMTD only). If TRUE, the printed summary includes the method-specific settings list. Default FALSE.
	Further arguments passed to or from other methods (ignored).

Details

An object of class "hdMTD" is an integer vector S (selected lags, elements of \mathbb{N}^+) with attributes:

- method: one of "FS", "FSC", "CUT", "BIC".
- d: upper bound for the order used in the call.
- call: the matched call that produced the object.
- settings: a (method-specific) list of the arguments actually used.
- A: the state space actually used (provided or inferred).
- (optional) BIC_selected_value for method="BIC" with BICvalue=TRUE.
- (optional) extras\$BIC_out for method="BIC" (exactly the output of hdMTD_BIC()).

print() shows the method, d, and the selected set of lags in \mathbb{N}^+ . summary() also prints the call, the state space used, the estimated lag set, optional BIC diagnostics, and the settings.

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Value

```
print.hdMTD Invisibly returns the "hdMTD" object.
summary.hdMTD An object of class "summary.hdMTD".
print.summary.hdMTD Invisibly returns the "summary.hdMTD" object.
```

See Also

```
hdMTD, hdMTD_FS, hdMTD_FSC, hdMTD_CUT, hdMTD_BIC, S, lags
```

Examples

```
## Not run:
set.seed(1)
M <- MTDmodel(Lambda = c(1, 4), A = c(1, 3), lam0 = 0.05)
X <- perfectSample(M, N = 400)
S_hat <- hdMTD(X, d = 5, method = "FS", l = 2)
print(S_hat)
summary(S_hat)
S(S_hat); lags(S_hat)
## End(Not run)</pre>
```

hdMTD_BIC

The Bayesian Information Criterion (BIC) method for inference in MTD models

Description

A function for estimating the relevant lag set Λ of a Markov chain using Bayesian Information Criterion (BIC). This means that this method selects the set of lags that minimizes a penalized log likelihood for a given sample, see *References* below for details on the method.

Usage

```
hdMTD_BIC(
    X,
    d,
    S = seq_len(d),
    minl = 1,
    maxl = length(S),
    xi = 1/2,
    A = NULL,
    byl = FALSE,
    BICvalue = FALSE,
    single_matrix = FALSE,
    indep_part = TRUE,
```

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```
zeta = maxl,
warn = FALSE,
...
)
```

Arguments

S

X A vector or single-column data frame containing a chain sample (X[1] is the most recent).

d A positive integer representing an upper bound for the chain order.

A numeric vector of positive integers from which this function will select a set of relevant lags. Typically, S is a subset of 1:d. If S is not provided, by default

S=1:d.

minl A positive integer. minl represents the smallest length of any relevant lag set this function might return. If minl == maxl, this function will return the subset of S of length minl with the lowest BIC. If minl < maxl, the function will consider

subsets ranging from length minl to length maxl when searching for the subset

of S with the smallest BIC.

max1 A positive integer equal to or greater than min1 but less than the number of elements in S (max1 = length(S) is accepted but in this case the output will al-

ways be S). max1 represents the largest length of any relevant lag set this function

might return.

xi The BIC penalization term constant. Defaulted to 1/2. A smaller xi (near 0)

reduces the impact of overparameterization.

A A vector with positive integers representing the state space. If not informed, this

function will set A=sort(unique(X)).

byl Logical. If TRUE, the function will look for the set with smallest BIC by each

length (from min1 to max1), and return the set with smallest BIC for each length. If min1==max1 setting by1=TRUE or FALSE makes no difference, since the function will only calculate the BIC for sets with max1 elements in the relevant lag

set.

BICvalue Logical. If TRUE, the function will also return the calculated values of the BIC

for the estimated relevant lag sets.

single_matrix Logical. If TRUE, the chain sample is thought to come from an MTD model

where the stochastic matrices p_j are constant across all lags $j \in \Lambda$. In practice, this means the user believes the stochastic matrices for every lag in S are the

same, which reduces the number of parameters in the penalization term.

indep_part Logical. If FALSE there is no independent distribution and $\lambda_0 = 0$ which reduces

the number of parameters in the penalization term.

zeta A positive integer representing the number of distinct matrices p_i in the MTD,

which affects the number of parameters in the penalization term. Defaulted to

max1. See more in *Details*.

warn Logical. If TRUE, the function warns the user when A is set automatically.

... Additional arguments (not used in this function, but maintained for compatibility

with hdMTD().

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Details

Criterion. For each candidate lag set T contained in S with size l = |T| where min1 <= 1 <= max1, hdMTD_BIC() evaluates

$$BIC(T) = -L_T + xi * df(T) * log(N),$$

where N = length(X) and

$$L_T = \sum_{x_T \in A^T} \sum_{a \in A} N(ax_T) * log(\hat{p}(a|x_T)).$$

The empirical conditionals are

$$\hat{p}(a|x_T) = N(ax_T)/N(x_T),$$

computed from the sample counts (same quantities returned by freqTab and empirical_probs).

Degrees of freedom. The parameter count df(T) is the number of free parameters of an MTD model with lag set T and state space A, honoring the constraints single_matrix, indep_part, and zeta:

$$df(T) = w_{df} + p0_{df} + |A| * (|A| - 1) * zeta.$$

Here zeta is the number of distinct p_j matrices allowed across lags (by default zeta=l; setting single_matrix = TRUE forces zeta=1). The weight and independent-part contributions are: $w_{df}=l$ if indep_part is TRUE, otherwise $w_{df}=l-1$; $p0_{df}=|A|-1$ if indep_part is TRUE, otherwise $p0_{df}=0$.

Scale. With xi = 1/2 (the default), BIC equals one half of the classical Schwarz BIC $-2 * L_T + df(T) * log(N)$; minimizing either criterion selects the same lag set.

Note. The likelihood term L_T sums over the N - max(T) effective transitions, while the penalty uses log(N) (this matches the implementation).

Note that the upper bound for the order of the chain (d) affects the estimation of the transition probabilities. If we run the function with a certain order parameter d, only the sequences of length d that appeared in the sample will be counted. Therefore, all transition probabilities, and hence all BIC values, will be calculated with respect to that d. If we use another value for d to run the function, even if the output agrees with that of the previous run, its BIC value might change a little.

The parameter zeta indicates the the number of distinct matrices p_j in the MTD. If zeta = 1, all matrices p_j are identical; if zeta = 2 there exists two groups of distinct matrices and so on. The largest value for zeta is maxl since this is the largest number of matrices p_j . When minl<maxl, for each minl < 1 < maxl, zeta = min(zeta, 1). If single_matrix = TRUE then zeta is set to 1.

Value

Returns a vector with the estimated relevant lag set using BIC. It might return more than one set if minl < maxl and byl = TRUE. Additionally, it can return the value of the penalized likelihood for the outputted lag sets if BICvalue = TRUE.

References

Imre Csiszár, Paul C. Shields. The consistency of the BIC Markov order estimator. *The Annals of Statistics*, 28(6), 1601-1619. doi:10.1214/aos/1015957472

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Examples

```
# Simulate a chain from an MTD model
set.seed(1)
M <- MTDmodel(Lambda = c(1, 3), A = c(1, 2), lam0 = 0.05)
X <- perfectSample(M, N = 400)

# Fit using BIC with a single lag
hdMTD_BIC(X, d = 6, minl = 1, maxl = 1)

# Fit using BIC with lag selection and extract BIC value
hdMTD_BIC(X, d = 3, minl = 1, maxl = 2, BICvalue = TRUE)</pre>
```

hdMTD_CUT

The CUT method for inference in MTD models

Description

A function that estimates the set of relevant lags of an MTD model using the CUT method.

Usage

```
hdMTD_CUT(
    X,
    d,
    S = seq_len(d),
    alpha = 0.05,
    mu = 1,
    xi = 0.5,
    A = NULL,
    warn = FALSE,
    ...
)
```

Arguments

X	A vector or single-column data frame containing a chain sample (X[1] is the most recent).
d	A positive integer representing an upper bound for the chain order.
S	A numeric vector of distinct positive integers from which this function will select a set of relevant lags. Should be a subset of 1:d. Default is 1:d.
alpha	A positive real number used in the CUT threshold (which determines if two distributions can be considered different). The larger the alpha, the greater the distance required to consider that there is a difference between a set of distributions.
mu	A positive real number such that ${\rm mu}>(e^{{\rm mu}}-1)/2.$ mu is also a component of the same threshold as alpha.

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xi	A positive real number, xi is also a component of the same threshold as alpha.
A	A vector with positive integers representing the state space. If not informed, this function will set $A \leftarrow sort(unique(X))$.
warn	Logical. If TRUE, the function warns the user when A is set automatically.
	Additional arguments (not used in this function, but maintained for compatibility with hdMTD().

Details

The "Forward Stepwise and Cut" (FSC) is an algorithm for inference in Mixture Transition Distribution (MTD) models. It consists in the application of the "Forward Stepwise" (FS) step followed by the CUT algorithm. This method and its steps where developed by Ost and Takahashi and are specially useful for inference in high-order MTD Markov chains. This specific function will only apply the CUT step of the algorithm and return an estimated relevant lag set.

Value

Returns a set of relevant lags estimated using the CUT algorithm.

References

Ost, G. & Takahashi, D. Y. (2023). Sparse Markov models for high-dimensional inference. *Journal of Machine Learning Research*, 24(279), 1-54. http://jmlr.org/papers/v24/22-0266.html

Examples

```
# Simulate a chain from an MTD model
set.seed(1)
M <- MTDmodel(Lambda = c(1, 4), A = c(1, 3), lam0 = 0.05)
X <- perfectSample(M, N = 400)

# Apply CUT with custom alpha, mu, and xi
hdMTD_CUT(X, d = 4, alpha = 0.02, mu = 1, xi = 0.4)

# Apply CUT with selected lags and smaller alpha
hdMTD_CUT(X, d = 6, S = c(1, 4, 6), alpha = 0.08)</pre>
```

hdMTD_FS

The Forward Stepwise (FS) method for inference in MTD models

Description

A function that estimates the set of relevant lags of an MTD model using the FS method.

Usage

```
hdMTD_FS(X, d, 1, A = NULL, elbowTest = FALSE, warn = FALSE, ...)
```

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Arguments

X	A vector or single-column data frame containing a chain sample (X[1] is the most recent).
d	A positive integer representing an upper bound for the chain order.
1	A positive integer specifying the number of lags to be selected as relevant.
A	A vector with positive integers representing the state space. If not informed, this function will set $A \leftarrow sort(unique(X))$.
elbowTest	Logical. If TRUE, the function applies an alternative stopping criterion to determine the length of the set of relevant lags. See <i>Details</i> for more information.
warn	Logical. If TRUE, the function warns the user when A is set automatically.
	Additional arguments (not used in this function, but maintained for compatibility with hdMTD().

Details

The "Forward Stepwise" (FS) algorithm is the first step of the "Forward Stepwise and Cut" (FSC) algorithm for inference in Mixture Transition Distribution (MTD) models. This method was developed by Ost and Takahashi This specific function will only apply the FS step of the algorithm and return an estimated relevant lag set of length 1.

This method iteratively selects the most relevant lags based on a certain quantity ν . In the first step, the lag in 1:d with the greatest ν is deemed important. This lag is included in the output, and using this knowledge, the function proceeds to seek the next important lag (the one with the highest ν among the remaining ones). The process stops when the output vector reaches length 1 if elbowTest=FALSE.

If elbowTest = TRUE, the function will store these maximum ν values at each iteration, and output only the lags that appear before the one with smallest ν among them.

Value

A numeric vector containing the estimated relevant lag set using FS algorithm.

References

Ost, G. & Takahashi, D. Y. (2023). Sparse Markov models for high-dimensional inference. *Journal of Machine Learning Research*, 24(279), 1-54. http://jmlr.org/papers/v24/22-0266.html

```
# Simulate a chain from an MTD model
set.seed(1)
M <- MTDmodel(Lambda = c(1, 3), A = c(1, 2), lam0 = 0.05)
X <- perfectSample(M, N = 400)

# Forward Stepwise with l = 2
hdMTD_FS(X, d = 5, l = 2)
# Forward Stepwise with l = 3</pre>
```

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```
hdMTD_FS(X, d = 4, 1 = 3)
```

hdMTD_FSC

Forward Stepwise and Cut method for inference in MTD models

Description

A function for inference in MTD Markov chains with FSC method. This function estimates the relevant lag set Λ of an MTD model through the FSC algorithm.

Usage

```
hdMTD_FSC(X, d, l, alpha = 0.05, mu = 1, xi = 0.5, A = NULL, ...)
```

Arguments

Х	A vector or single-column data frame containing a chain sample (X[1] is the most recent).
d	A positive integer representing an upper bound for the chain order.
1	A positive integer that sets the number of elements in the output vector.
alpha	A positive real number used in the CUT threshold (which determines if two distributions can be considered different). The larger the alpha, the greater the distance required to consider that there is a difference between a set of distributions. Defaulted to 0.05.
mu	A positive real number such that ${\rm mu}>(e^{{\rm mu}}-1)/2.$ mu is also a component of the same threshold as alpha.
xi	A positive real number, xi is also a component of the same threshold as alpha.
Α	A vector with positive integers representing the state space. If not informed, this function will set A <- sort(unique(X)).
	Additional arguments (not used in this function, but maintained for compatibility with hdMTD().

Details

The "Forward Stepwise and Cut" (FSC) is an algorithm for inference in Mixture Transition Distribution (MTD) models. It consists in the application of the "Forward Stepwise" (FS) step followed by the CUT algorithm. This method and its steps where developed by Ost and Takahashi and are specially useful for inference in high-order MTD Markov chains.

Value

Returns a vector with the estimated relevant lag set using FSC algorithm.

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References

Ost, G. & Takahashi, D. Y. (2023). Sparse Markov models for high-dimensional inference. *Journal of Machine Learning Research*, 24(279), 1-54. http://jmlr.org/papers/v24/22-0266.html

Examples

```
# Simulate a chain from an MTD model set.seed(1) M <- MTDmodel(Lambda = c(1, 3), A = c(1, 2), lam0 = 0.05) X <- perfectSample(M, N = 400) # Forward Stepwise and Cut with different parameters hdMTD_FSC(X, d = 4, 1 = 2) hdMTD_FSC(X, d = 4, 1 = 3, alpha = 0.1)
```

MTD-accessors

Accessors for objects of classes "MTD", "MTDest", and "hdMTD"

Description

Public accessors that expose model components without relying on the internal list structure. These accessors are available for "MTD" (model objects), "MTDest" (EM fits), and "hdMTD" (lag selection), except transitP() which only applies to "MTD".

Usage

```
pj(object)

p0(object)

lambdas(object)

lags(object)

Lambda(object)

S(object)

states(object)

transitP(object)

## S3 method for class 'MTD' pj(object)

## S3 method for class 'MTD'
```

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```
p0(object)
## S3 method for class 'MTD'
lambdas(object)
## S3 method for class 'MTD'
lags(object)
## S3 method for class 'MTD'
Lambda(object)
## S3 method for class 'MTD'
states(object)
## S3 method for class 'MTD'
transitP(object)
## S3 method for class 'MTDest'
pj(object)
## S3 method for class 'MTDest'
p0(object)
## S3 method for class 'MTDest'
lambdas(object)
## S3 method for class 'MTDest'
lags(object)
## S3 method for class 'MTDest'
S(object)
## S3 method for class 'MTDest'
states(object)
## S3 method for class 'hdMTD'
S(object)
## S3 method for class 'hdMTD'
lags(object)
```

Arguments

object An object of class "MTD", "MTDest" or "hdMTD" (as supported by each accessor).

Details

Returned lag sets follow the package convention and are shown as negative integers via lags() (elements of \mathbb{Z}^-). For convenience, positive-index accessors are also provided: Lambda() for "MTD"

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objects and S() for "MTDest" and "hdMTD" objects (elements of \mathbb{N}^+). Internally, lags may be stored as positive integers in Lambda or S.

For computing the global transition matrix of an EM fit the user can first coerce the MTDest object into an MTD using as.MTD and then access the matrix with transitP(as.MTD(object)).

Value

```
pj(object) A list of stochastic matrices (one per lag). p\emptyset(\text{object}) \text{ A numeric probability vector for the independent component.} \\ \text{lambdas(object)} \text{ A numeric vector of mixture weights that sums to 1.} \\ \text{lags(object)} \text{ The lag set (elements of } \mathbb{Z}^-). \\ \text{Lambda(object)} \text{ For "MTD", the lag set as positive integers (elements of } \mathbb{N}^+). \\ \text{S(object)} \text{ For "MTDest" and "hdMTD", the lag set as positive integers (elements of } \mathbb{N}^+). \\ \text{states(object)} \text{ The state space.} \\ \text{transitP(object)} \text{ For "MTD" objects only, the global transition matrix } P. \text{ Not available for "MTDest".} \\ }
```

See Also

```
MTDmodel, MTDest, hdMTD, as.MTD
```

```
## Not run:
## For generating an MTD model
set.seed(1)
m <- MTDmodel(Lambda = c(1, 3), A = c(0, 1))
pj(m); p0(m); lambdas(m); lags(m); Lambda(m); states(m)
transitP(m)
## For an EM fit (using coef(m) as init for simplicity):
X <- perfectSample(m, N = 800)
fit <- MTDest(X, S = c(1, 3), init = coef(m))
pj(fit); p0(fit); lambdas(fit); lags(fit); S(fit); states(fit)
transitP(as.MTD(fit))
## For lag selection:
S_hat <- hdMTD(X, d = 5, method = "FS", l = 2)
S(S_hat); lags(S_hat)
## End(Not run)</pre>
```

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|--|

Description

Printing, summarizing, and coefficient-extraction methods for Mixture Transition Distribution (MTD) model objects.

Usage

```
## S3 method for class 'MTD'
print(x, ...)

## S3 method for class 'MTD'
summary(object, ...)

## S3 method for class 'summary.MTD'
print(x, ...)

## S3 method for class 'MTD'
coef(object, ...)

## S3 method for class 'MTD'
logLik(object, X, ...)
```

Arguments

```
    An object of class "MTD" or "summary.MTD", depending on the method.
    Further arguments passed to or from other methods (ignored).
    An object of class "MTD".
    A vector or single-column data frame containing an MTD chain sample (values must be in the model's state space).
```

Details

print.MTD() displays the relevant lag set (shown as negative integers) and the state space. For a detailed overview including mixture weights and a compact preview of the global transition matrix P, use summary().

Value

```
print.MTD Invisibly returns the "MTD" object, after displaying its relevant lag set and state space.
summary.MTD An object of class "summary.MTD" with fields: order, states, lags, indep, lambdas, p0 (or NULL), P_dim, and P_head.
print.summary.MTD Invisibly returns the "summary.MTD" object after printing its contents.
coef.MTD A list with model parameters: lambdas, pj, and p0.
```

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logLik.MTD An object of class "logLik" with attributes nobs (number of transitions) and df (free parameters), honoring model constraints such as single_matrix and the independent component (indep_part).

See Also

MTDmodel, MTDest, transitP, lambdas, pj, p0, lags, Lambda, states, summary.MTDest, coef.MTDest, oscillation, perfectSample, logLik

Examples

```
## Not run:
set.seed(1)
m <- MTDmodel(Lambda = c(1, 3), A = c(0, 1), lam0 = 0.05)

print(m)  # compact display: lags (Z^-) and state space
s <- summary(m)
print(s)

coef(m)  # list(lambdas = ..., pj = ..., p0 = ...)
transitP(m)  # global transition matrix P
pj(m); p0(m); lambdas(m); lags(m); Lambda(m); states(m)

## End(Not run)</pre>
```

MTDest

EM estimation of MTD parameters

Description

Estimation of MTD parameters through the Expectation Maximization (EM) algorithm.

Usage

```
MTDest(
   X,
   S,
   M = 0.01,
   init,
   iter = FALSE,
   nIter = 100,
   A = NULL,
   oscillations = FALSE
)
```

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Arguments

Χ	A vector or single-column data frame containing an MTD chain sample (X[1] is the most recent).
S	A numeric vector of distinct positive integers, sorted increasingly. Typically, S represents a set of relevant lags.
М	A stopping point for the EM algorithm. If M=NULL the algorithm will run for a total of nIter iterations (i.e., no convergence check).
init	A list with initial parameters: p0 (optional), lambdas (required), pj (required). The entries in lambdas are weights for the distribution p0 and the distributions present in the list pj. Therefore, the order in which the elements appear in the vector lambdas is important for correct assignment. See <i>Details</i> .
iter	Logical. If TRUE include iteration diagnostics in the output (number of updates iterations; vector of absolute log-likelihood changes deltaLogLik; and lastComputedDelta, the last delta log-likelihood compared against M).
nIter	An integer positive number with the maximum number of EM iterations.
Α	Optional integer vector giving the state space. If omitted, defaults to sort(unique(X)).
oscillations	Logical. If TRUE, also compute oscillations for the fitted model (see oscillation).

Details

Regarding the M parameter: it functions as a stopping criterion within the EM algorithm. When the difference between the log-likelihood computed with the newly estimated parameters and that computed with the previous parameters falls below M, the algorithm halts. Nevertheless, if the value of nIter (which represents the maximum number of iterations) is smaller than the number of iterations required to meet the M criterion, the algorithm will conclude its execution when nIter is reached. To ensure that the M criterion is effectively utilized, we recommend using a higher value for nIter, which is set to a default of 100.

Concerning the init parameter, it is expected to be a list with 2 or 3 entries. These entries consist of: an optional vector named p0, representing an independent distribution (the probability in the first entry of p0 must be that of the smallest element in A and so on), a required list of matrices pj, containing a stochastic matrix for each element of S (the first matrix corresponds to the smallest lag in S and so on), and a vector named lambdas representing the weights, the first entry must be the weight for p0, and then one entry for each element in pj list. If your MTD model does not have an independent distribution p0, set init\$lambdas[1]=0.

Value

An S3 object of class "MTDest" (a list) with at least the following elements:

- lambdas: estimated mixture weights (independent part first, if any).
- pj: list of estimated transition matrices p_i .
- p0: estimated independent distribution (if applicable).
- logLik: log-likelihood of the final fitted model.

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• iterations, deltaLogLik, lastComputedDelta (optional): returned if iter = TRUE. Here, iterations is the number of parameter updates performed; deltaLogLik stores the successive absolute log-likelihood changes for the accepted updates; and lastComputedDelta is the last computed change (which may be below M when the loop stops by convergence).

- oscillations (optional): returned if oscillations = TRUE.
- call: the matched call.
- S: the lag set used for estimation.
- A: the state space used for estimation.
- n: the sample size.
- n_eff: the effective sample size used for estimation.

References

Lebre, Sophie and Bourguignon, Pierre-Yves. (2008). An EM algorithm for estimation in the Mixture Transition Distribution model. *Journal of Statistical Computation and Simulation*, 78(1), 1-15. doi:10.1080/00949650701266666

See Also

Methods for fitted objects: print.MTDest, summary.MTDest, print.summary.MTDest, coef.MTDest, logLik.MTDest. Model constructor and related utilities: MTDmodel, oscillation. Coercion helper: as.MTD

```
# Simulating data.
set.seed(1)
MTD <- MTDmodel(Lambda = c(1, 10), A = c(0, 1), lam0 = 0.01)
X <- perfectSample(MTD, N = 400)</pre>
# Initial Parameters:
init <- list(</pre>
  'p0' = c(0.4, 0.6),
  'lambdas' = c(0.05, 0.45, 0.5),
  'pj' = list(
      matrix(c(0.2, 0.8, 0.45, 0.55), byrow = TRUE, ncol = 2),
      matrix(c(0.25, 0.75, 0.3, 0.7), byrow = TRUE, ncol = 2)
    )
 )
fit <- MTDest(X, S = c(1, 10), init = init, iter = TRUE)
str(fit, max.level = 1)
fit$logLik
fit2 <- MTDest(X, S = c(1, 10), init = init, oscillations = TRUE)
fit2$oscillations
```

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MTDest-methods

Methods for objects of class "MTDest"

Description

Printing method for EM fits of Mixture Transition Distribution (MTD) models.

Summary method for EM fits of MTD models.

Printing method for "summary.MTDest" objects.

Extract coefficients from an "MTDest" fit.

Extract log-likelihood from an "MTDest" fit.

Usage

```
## S3 method for class 'MTDest'
print(x, ...)

## S3 method for class 'MTDest'
summary(object, ...)

## S3 method for class 'summary.MTDest'
print(x, ...)

## S3 method for class 'MTDest'
coef(object, ...)

## S3 method for class 'MTDest'
logLik(object, ...)
```

Arguments

x An object of class "MTDest" or "summary.MTDest", depending on the method.

... Further arguments passed to or from other methods (ignored).

An object of class "MTDest" (used by methods that operate on the fitted model).

Details

The print.MTDest() method displays a compact summary of the fitted model: the lag set (S), the state space (A), the final log-likelihood, and, if available, the number of EM updates performed.

The summary.MTDest() method collects key fields from an "MTDest" object into a compact list (class "summary.MTDest") suitable for printing.

The print.summary.MTDest() method prints that summary in a readable format, including lambdas, transition matrices, independent distribution, log-likelihood, oscillations (if available), and iteration diagnostics (if available).

The coef.MTDest() method returns the fitted mixture weights (lambdas), the list of transition matrices (pj), and (if present) the independent distribution p0.

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The logLik.MTDest() computes the log-likelihood and returns an object of class "logLik" with attributes: nobs, the effective sample size used for estimation, and df, number of free parameters estimated supposing all transition matrices pj to be distinct (multimatrix model). Note: in the returned "logLik" object, df denotes the number of free parameters (not residual degrees of freedom).

Value

print.MTDest Invisibly returns the "MTDest" object, after displaying its lag set, state space, final log-likelihood, and iteration count (if available).

print.summary.MTDest Invisibly returns the "summary.MTDest" object, after displaying its contents: lambdas; transition matrices; independent distribution; log-likelihood; oscillations (if available); and iteration diagnostics (if available).

summary.MTDest An object of class "summary.MTDest".

coef.MTDest A list with estimated lambdas, pj, and p0.

logLik.MTDest An object of class "logLik" with attributes df (number of free parameters) and nobs (effective sample size).

See Also

MTDest, summary.MTDest, print.summary.MTDest, coef.MTDest, logLik, AIC, BIC

Examples

```
set.seed(1)
MTD <- MTDmodel(Lambda = c(1, 3), A = c(0, 1), lam0 = 0.01)
X <- perfectSample(MTD, N = 200)  # small N to keep examples fast
init <- list(
    p0 = c(0.4, 0.6),
    lambdas = c(0.05, 0.45, 0.5),
    pj = list(
        matrix(c(0.2, 0.8, 0.45, 0.55), byrow = TRUE, ncol = 2),
        matrix(c(0.25, 0.75, 0.3, 0.7), byrow = TRUE, ncol = 2)
    )
)
fit <- MTDest(X, S = c(1, 3), init = init, iter = TRUE)
print(fit)
summary(fit)
coef(fit)
logLik(fit)
BIC(fit)</pre>
```

MTDmode1

Creates a Mixture Transition Distribution (MTD) Model

Description

Generates an MTD model as an object of class MTD given a set of parameters.

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Usage

```
MTDmodel(
  Lambda,
  A,
  lam0 = NULL,
  lamj = NULL,
  pj = NULL,
  p0 = NULL,
  single_matrix = FALSE,
  indep_part = TRUE
)
```

Arguments

Lambda	A numeric vector of positive integers representing the relevant lag set. The elements will be sorted from smallest to greatest. The smallest number represents the latest (most recent) time in the past, and the largest number represents the earliest time in the past.
Α	A vector with nonnegative integers representing the state space.
lam0	A numeric value in $[0,1)$, representing the weight of the independent distribution.
lamj	A numeric vector of weights for the transition probability matrices in pj. Values must be in the range [0, 1), and their sum with lam0 must be equal to 1. The first element in lamj must be the weight for the first element in Lambda and so on.
pj	A list with length(Lambda) stochastic matrices, each of size length(A) \times length(A). The first matrix in pj must refer to the first element in Lambda and so on.
p0	A probability vector for the independent component of the MTD model. If NULL and indep_part=TRUE, the distribution will be sampled from a uniform distribution. If indep_part=FALSE, then there is no independent distribution and p0 entries will be set to zero. If you enter p0=0, indep_part is set to FALSE.
single_matrix	Logical. If TRUE, all matrices in list pj are identical.
indep_part	Logical. If FALSE, the model does not include an independent distribution and p0 is set to zero.

Details

The resulting MTD object can be used by functions such as oscillation(), which retrieves the model's oscillation, and perfectSample(), which will sample an MTD Markov chain from its invariant distribution.

Value

A list of class MTD containing:

P The transition probability matrix of the MTD model. lambdas A vector with MTD weights (lam0 and lamj).

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```
pj A list of stochastic matrices defining conditional transition probabilities.
```

p0 The independent probability distribution.

Lambda The vector of relevant lags.

A The state space.

single_matrix A logical argument, if TRUE indicates that all matrices in pj are identical.

Examples

```
summary(MTDmodel(Lambda=c(1,3),A=c(4,8,12)))

MM <- MTDmodel(Lambda=c(2,4,9),A=c(0,1),lam0=0.05,lamj=c(0.35,0.2,0.4),
pj=list(matrix(c(0.5,0.7,0.5,0.3),ncol=2)),p0=c(0.2,0.8),single_matrix=TRUE)
transitP(MM); pj(MM); oscillation(MM)

MM <- MTDmodel(Lambda=c(2,4,9),A=c(0,1),lam0=0.05,
pj=list(matrix(c(0.5,0.7,0.5,0.3),ncol=2)),single_matrix=TRUE,indep_part=FALSE)
p0(MM); lambdas(MM)</pre>
```

oscillation

Oscillations of an MTD Markov chain

Description

Calculates the oscillations of an MTD model object or estimates the oscillations of a chain sample.

Usage

```
scillation(x, ...)
## S3 method for class 'MTD'
oscillation(x, ...)
## Default S3 method:
oscillation(x, S, A = NULL, ...)
```

Arguments

- x Must be an MTD object or a chain sample.
- ... Ignored.
- S A numeric vector of distinct positive integers. Represents a set of lags.
- A Optional integer vector giving the state space. If omitted, defaults to sort(unique(x)).

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Details

For an MTD model, the oscillation for lag j ($\{\delta_j: j \in \Lambda\}$), is the product of the weight λ_j multiplied by the maximum of the total variation distance between the distributions in a stochastic matrix p_j .

$$\delta_j = \lambda_j \max_{b,c \in \mathcal{A}} d_{TV}(p_j(\cdot|b), p_j(\cdot|c)).$$

So, if x is an MTD object, the parameters Λ , \mathcal{A} , λ_j , and p_j are inputted through, respectively, the entries Lambda, A, lambdas and the list pj of stochastic matrices. Hence, an oscillation δ_j may be calculated for all $j \in \Lambda$. For estimating the oscillations from a sample, then x must be a chain, and S, a vector representing a set of lags, must be informed. This way the transition probabilities can be estimated.

Let $\hat{p}(\cdot|x_S)$ symbolize an estimated distribution in \mathcal{A} given a certain past x_S (which is a sequence of elements of \mathcal{A} where each element occurred at a lag in S), and $\hat{p}(\cdot|b_jx_S)$ an estimated distribution given past x_S and that the symbol $b \in \mathcal{A}$ occurred at lag j. If N is the sample size, $d = \max(S)$ and $N(x_S)$ is the number of times the sequence x_S appeared in the sample, then

$$\delta_{j} = \max_{c_{j}, b_{j} \in \mathcal{A}} \frac{1}{N - d} \sum_{x_{S} \in \mathcal{A}^{S}} N(x_{S}) d_{TV}(\hat{p}(.|b_{j}x_{S}), \hat{p}(.|c_{j}x_{S}))$$

is the estimated oscillation for a lag $j \in \{1, \dots, d\} \setminus S$. Note that \mathcal{A}^S is the space of sequences of \mathcal{A} indexed by S.

Value

A named numeric vector of oscillations. If the x parameter is an MTD object, it will provide the oscillations for each element in Lambda. If x is a chain sample, it estimates the oscillations for a user-inputted set of lags S.

Methods (by class)

- oscillation(MTD): For an MTD object: computes δ_i for all $j \in \Lambda$.
- oscillation(default): For a chain sample: estimates δ_j for each j in S.

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perfectSample

Perfectly samples an MTD Markov chain

Description

Samples an MTD Markov Chain from the stationary distribution.

Usage

```
perfectSample(MTD, N = NULL)
```

Arguments

MTD An MTD object, see MTDmodel() for properly generating a MTD object.

N The sample size. If NULL sample size will be set to 1000.

Details

This perfect sample algorithm requires that the MTD model has an independent distribution (p0) with a positive weight (i.e., MTD\$lambdas["lam0"]>0 which means $\lambda_0 > 0$).

Value

Returns a sample from an MTD model (the first element is the most recent).

Examples

```
perfectSample(MTDmodel(Lambda=c(1,4), A = c(0,2)), N = 200 ) perfectSample(MTDmodel(Lambda=c(2,5), A = c(1,2,3)), N = 1000 )
```

probs

Predictive probabilities for MTD / MTDest

Description

Compute one-step-ahead predictive probabilities under an MTD model or an MTDest fit.

Conventions:

- Samples are read most recent first: $x[1] = X_{t-1}, x[2] = X_{t-2}$, etc.
- The global transition matrix P is indexed by row labels that list the past context from oldest to newest. A cell at row "s_k...s_1" and column "a" is read as p(a | s_1...s_k).
- If both newdata and context are missing, probs() returns the full global transition matrix (transitP(object) for MTD; transitP(as.MTD(object)) for MTDest).

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Usage

```
probs(object, context = NULL, newdata = NULL, oldLeft = FALSE)
## S3 method for class 'MTD'
probs(object, context = NULL, newdata = NULL, oldLeft = FALSE)
## S3 method for class 'MTDest'
probs(object, context = NULL, newdata = NULL, oldLeft = FALSE)
```

Arguments

object An MTD or MTDest object.

context Optional vector or matrix/data.frame of contexts (rows). By default, each row

follows the "most recent first" convention; set oldLeft = TRUE if rows are supplied oldest to newest. Must have exactly length(Lambda(object)) columns

for MTD or length(S(object)) for MTDest (one symbol per lag).

newdata Optional vector or matrix/data.frame of samples (rows). Columns follow the

"most recent first" convention. Must have at least max(Lambda(object)) columns for MTD or max(S(object)) for MTDest. Only one of newdata or context can be provided at a time. When there are extra columns, only the columns at the

model lags are used.

oldLeft Logical. If TRUE, interpret rows in newdata/context as oldest to newest (e.g.

leftmost = newdata[,1] = oldest). If FALSE (default), rows are most recent

first.

Details

All entries of newdata/context must belong to the model's state space states(object). For MTDest, returning the full matrix materializes transitP(as.MTD(object)), which can be large for big state spaces or many lags.

Value

A numeric matrix of predictive probabilities with one row per input context and columns indexed by states(object). Row names are the context labels (oldest to newest) formed by concatenating state symbols without a separator. If both newdata and context are missing, the full global transition matrix is returned.

See Also

```
transitP, states, Lambda, S, as.MTD, empirical_probs
```

```
set.seed(1)
m <- MTDmodel(Lambda = c(1,3), A = c(0,1), lam0 = 0.1)
# Full matrix
P <- probs(m)</pre>
```

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```
# Using a sample row (most recent first): newdata has >= max(Lambda) columns
new_ctx <- c(1, 0, 1, 0)  # X_{t-1}=1, X_{t-2}=0, X_{t-3}=1, ...
probs(m, newdata = new_ctx)  # one row of probabilities

# Explicit contexts (exactly |Lambda| symbols per row)
probs(m, context = c(0, 1), oldLeft = FALSE)  # most recent first
probs(m, context = c(0, 1), oldLeft = TRUE)  # oldest to newest

# Multiple contexts (rows)
ctxs <- rbind(c(1,0,1), c(0,1,1), c(1,1,0))
probs(m, newdata = ctxs)</pre>
```

tempdata

Maximum temperatures in the city of Brasília, Brazil.

Description

A data frame with the maximum temperature of the last hour, by each hour, in the city of Brasília, Brazil. The data spans from 01/01/2003 to 31/08/2024.

Usage

tempdata

Format

A data frame with 189936 rows and 3 columns. Each row corresponds to a time in a day specified in columns 2 ("TIME") and 1 ("DATE") respectively. The value in column 3 ("MAXTEMP") is the maximum temperature measured in the last hour, in Celsius (C°), in the city of Brasília, the capital of Brazil, located in the central-western part of the country.

DATE The day, from 01/01/2003 to 31/08/2024

TIME The time, form 00:00 to 23:00 each day

MAXTEMP The maximum temperature measured in the last hour in Celsius

Source

Meteorological data provided by INMET (National Institute of Meteorology, Brazil). Data collected from automatic weather station in Brasília (latitude: -15.79°, longitude: -47.93°, altitude: 1159.54 m). Available at: https://bdmep.inmet.gov.br/

```
data(tempdata)
```

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