# Package 'changepointGA'

September 28, 2025

Type Package

Title Changepoint Detection via Modified Genetic Algorithm

**Version** 0.1.3 **Date** 2025-09-26

Description The Genetic Algorithm (GA) is used to perform changepoint analysis in time series data. The package also includes an extended island version of GA, as described in Lu, Lund, and Lee (2010, <doi:10.1214/09-AOAS289>). By mimicking the principles of natural selection and evolution, GA provides a powerful stochastic search technique for solving combinatorial optimization problems. In 'changepointGA', each chromosome represents a changepoint configuration, including the number and locations of changepoints, hyperparameters, and model parameters. The package employs genetic operators—selection, crossover, and mutation—to iteratively improve solutions based on the given fitness (objective) function. Key features of 'changepointGA' include encoding changepoint configurations in an integer format, enabling dynamic and simultaneous estimation of model hyperparameters, changepoint configurations, and associated parameters. The detailed algorithmic implementation can be found in the package vignettes and in the paper of Li (2024, <doi:10.48550/arXiv.2410.15571>).

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# Description

AMOCcrossover

In this crossover operator designed for AMOC problem, the new child is produced by taking the average of the changepoint locations from dad and mom and round to an integer. Note, every chromosome has at most one candidate changepoint location.

Average crossover operator to produce offspring for AMOC problem

# Usage

```
AMOCcrossover(mom, dad, prange = NULL, minDist, lmax, N)
```

AMOCmutation 3

# **Arguments**

mom	Among two selected individuals, mom represents the selected chromosome representation with lower fitness function value.
dad	Among two selected individuals, dad represents the selected chromosome representation with larger fitness function value.
prange	The default value is NULL. If there is no requirement on model order selection, such an auxiliary argument is needed for GA and IslandGA functions.
minDist	The minimum length between two adjacent changepoints.
lmax	The maximum possible length of the chromosome representation.
N	The length of time series.

# Value

The child chromosome that produced from mom and dad for next generation.

AMOCmutation	Jump mutation operator to produce offspring for AMOC problem

# **Description**

In a certain probability, the mutation genetic operator can be applied to generate a new child. In this AMOC mutation operator, the new child changepoint location can be down via a "jump" method. The child changepoint location will jump minDist time units either to the left or right to produce the changepoint location for the mutated child. The jump direction is randomly decided with 0.5 probability.

# Usage

```
AMOCmutation(
  child,
  prange = NULL,
  minDist,
  pchangepoint = NULL,
  lmax = NULL,
  mmax = NULL,
  N = NULL
)
```

# **Arguments**

child	The child chromosome resulting from the crossover genetic operator.
prange	The default value is NULL. If there is no requirement on model order selection, such an auxiliary argument is needed for GA and IslandGA functions.
minDist	The minimum length between two adjacent changepoints in AMOCselection operator, which is also the jump magnitude in the AMOCmutation operator.

4 AMOC population

pchangepoint	An auxiliary argument is needed for GA and IslandGA functions.
lmax	An auxiliary argument is needed for GA and IslandGA functions.
mmax	An auxiliary argument is needed for GA and IslandGA functions.
N	An auxiliary argument is needed for GA and IslandGA functions.

## Value

The resulting child chromosome representation.

AMOCpopulation	Random population initialization for AMOC problem	

# **Description**

Randomly generate the individuals' chromosomes (changepoint configurations) to construct the first generation population for the at most one changepoint (AMOC) problem.

# Usage

```
AMOCpopulation(popSize, prange, N, minDist, pchangepoint, mmax, lmax)
```

## **Arguments**

popSize	An integer rer	presents the n	umber of in	ndividual in	each po	pulation for	: GA (c	or

subpopulation for IslandGA).

prange Default is NULL for only changepoint detection. If prange is specified as a list

object, which contains the range of each model order parameters for order selection (integers). The number of order parameters must be equal to the length

of prange.

N The length of time series.

minDist The minimum length between two adjacent changepoints.

pchangepoint The probability that a changepoint can occur.

mmax The maximum possible number of changepoints in the data set.

1max The maximum possible length of the chromosome representation.

# **Details**

Given the possible candidate changepoint location set, each chromosome in the first generation population can be obtained by randomly sampling one location from the candidate set. The first element of every chromosome represent the number of changepoints and the last non-zero element always equal to the length of time series plus one (N+1).

## Value

A matrix that contains each individual's chromosome.

AMOCselection 5

AMOCselection	The parents selection genetic algorithm operator for AMOC problem
AMOCselection	The parents selection genetic algorithm operator for AMOC problem

## **Description**

The genetic algorithm require to select a pair of chromosomes, representing dad and mom, for the crossover operator to produce offspring (individual for next generation). Here, the same linear ranking method in selection\_linearrank is used to select a pair of chromosomes for dad and mom in the at most one changepoint (AMOC) problem. By default, the dad has better fit/smaller fitness function value/larger rank than mom.

# Usage

```
AMOCselection(pop, popFit)
```

# **Arguments**

pop A matrix contains the chromosomes for all individuals. The number of rows is

equal to lmax and the number of columns is equal to the popSize.

popFit A vector contains the objective function value (population fit) being associated

to each individual chromosome from above.

## Value

A list contains the chromosomes for dad and mom.

mple function: Calculating BIC for AR(1) model
mple function: Calculating BIC for AR(1) model

# Description

The objective function for changepoint search in Autoregressive moving average with model order selection via Bayesian Information Criterion (BIC).

## Usage

```
ARIMA.BIC(chromosome, plen = 0, XMat, Xt)
```

# **Arguments**

chromosome The chromosome consists of the number of changepoints, the order of AR part,

the order of MA part, the changepoint locations, and a value of time series length

plus 1 (N+1) indicating the end of the chromosome.

plen The number of model order parameters that need to be selected. If model order

selection needs to be performed simultaneously with the changepoint detection

task, plen should be nonzero.

6 ARIMA.BIC.Order

XMat A matrix contains the covariates, but not includes changepoint effects, for time series regression.

Xt The simulated ARMA time series from ts.sim function.

## Value

The BIC value of the objective function.

## **Examples**

```
Ts <- 1000
betaT <- c(0.5) # intercept
XMatT <- matrix(1, nrow = Ts, ncol = 1)</pre>
colnames(XMatT) <- "intercept"</pre>
sigmaT <- 1
phiT <- c(0.5)
thetaT <- NULL
DeltaT <- c(2, -2)
Cp.prop <- c(1 / 4, 3 / 4)
CpLocT <- floor(Ts * Cp.prop)</pre>
myts <- ts.sim(</pre>
  beta = betaT, XMat = XMatT, sigma = sigmaT, phi = phiT, theta = thetaT,
  Delta = DeltaT, CpLoc = CpLocT, seed = 1234
)
# candidate changepoint configuration
chromosome \leftarrow c(2, 250, 750, 1001)
ARIMA.BIC(chromosome, XMat = XMatT, Xt = myts)
```

ARIMA.BIC.Order

Calculating BIC for Multiple changepoint detection with model order selection

#### **Description**

The objective function for changepoint search in Autoregressive moving average with model order selection via Bayesian Information Criterion (BIC).

# Usage

```
ARIMA.BIC.Order(chromosome, plen = 2, XMat, Xt)
```

## **Arguments**

chromosome

A vector consists of the number of changepoints, the order of AR component (refers to the number of lagged terms used to model the current value of a time series), the order of MA component (refers to the number of lagged error terms used to model the current value of a time series), the changepoint locations,

cptDist 7

	and a value of time series sample size plus 1 (\$N+1\$) indicating the end of the chromosome.
plen	The number of model order parameters that need to be selected. If model order selection needs to be performed simultaneously with the changepoint detection task, plen should be nonzero.
XMat	A matrix contains the covariates, but not includes changepoint effects, for time series regression.
Xt	The simulated ARMA time series from ts.sim function.

## Value

The BIC value of the objective function.

# **Examples**

```
N <- 1000
XMatT <- matrix(1, nrow = N, ncol = 1)
Xt <- ts.sim(
  beta = 0.5, XMat = XMatT, sigma = 1, phi = 0.5, theta = 0.8,
  Delta = c(2, -2), CpLoc = c(250, 750), seed = 1234
)
# one chromosome representation
chromosome <- c(2, 1, 1, 250, 750, 1001)
ARIMA.BIC.Order(chromosome, plen = 2, XMat = XMatT, Xt = Xt)</pre>
```

 ${\tt cptDist}$ 

Comparing multiple changepoint configurations by pairwise distance

# **Description**

This function is to calculate the distance metric (Shi et al., 2022) between two changepoint configurations,  $C_1 = \{\tau_1, \dots, \tau_m\}$  and  $C_2 = \{\eta_1, \dots, \eta_k\}$ , where  $\tau$ 's are the changepoint locations.

# Usage

```
cptDist(tau1, tau2, N)
```

# Arguments

tau1	A vector contains the changepoint locations for $C_1$ for comparison. A value NULL is required if there is no changepoint detected.
tau2	A vector contains the changepoint locations for ${\cal C}_2$ for comparison. A value NULL is required if there is no changepoint detected.
N	The simulated time series sample size. Two changepoint configurations should have the same $n$ values.

#### **Details**

The pairwise distance was proposed by Shi et al. (2022),

$$d(C_1, C_2) = |m - k| + \min(A(C_1, C_2)),$$

where m is the number of changepoints in configuration  $C_1$  and k is the number of changepoints in configuration  $C_2$ . The term  $\min(A(C_1,C_2))$  reflects the cost of matching changepoint locations between  $C_1$  and  $C_2$  and can be calculated using the linear assignment method. Details can be found in Shi et al. (2022). Note: if one configuration doesn't contain any changepoints (valued NULL), the distance is defined as |m-k|. The function can also be used to examine changepoint detection performance in simulation studies. Given the true changepoint configuration,  $C_{true}$ , used in generating the time series, the calculated distance between the estimated multiple changepoint configuration,  $C_{est} = \{\eta_1, \ldots, \eta_k\}$ , and  $C_{true}$  can be used to evaluate the performance of the detection algorithm.

#### Value

dist

The calculated distance.

#### References

Shi, X., Gallagher, C., Lund, R., & Killick, R. (2022). A comparison of single and multiple change-point techniques for time series data. *Computational Statistics & Data Analysis*, 170, 107433.

#### **Examples**

```
N <- 100

# both tau1 and tau2 has detected changepoints
tau2 <- c(25, 50, 75)
tau1 <- c(20, 35, 70, 80, 90)
cptDist(tau1 = tau1, tau2 = tau2, N = N)

# either tau1 or tau2 has zero detected changepoints
cptDist(tau1 = tau1, tau2 = NULL, N = N)
cptDist(tau1 = NULL, tau2 = tau2, N = N)

# both tau1 and tau2 has zero detected changepoints
cptDist(tau1 = NULL, tau2 = NULL, N = N)</pre>
```

cptga

Genetic algorithm

#### **Description**

Perform the genetic algorithm for changepoint detection. This involves the minimization of an objective function using a genetic algorithm (GA). The algorithm can be run sequentially or with explicit parallelization.

## Usage

```
cptga(
  ObjFunc,
 Ν,
  prange = NULL,
 popSize = 200,
  pcrossover = 0.95,
  pmutation = 0.3,
  pchangepoint = 0.01,
 minDist = 1,
 mmax = NULL,
  1max = NULL,
 maxgen = 50000,
 maxconv = 5000,
 option = "cp",
 monitoring = FALSE,
 parallel = FALSE,
  nCore = NULL,
  tol = 1e-05,
  seed = NULL,
  popInitialize = "random_population",
  suggestions = NULL,
  selection = "selection_linearrank",
  crossover = "uniformcrossover",
 mutation = "mutation",
)
```

# Arguments

ObjFunc

The fitness function to be minimized. Users can specify any R or Rcpp function as the fitness function, setting the input as the potential solution to the optimization problem and returning a numerical value as the output/fitness. Depending on the user-specified chromosome representation, the optimization task can be changepoint detection only or changepoint detection plus model order selection, which can be specified via the option parameter. When option="both", the list prange must be specified to give the range of model orders.

N The sample size of the time series.

prange

The default value is NULL for changepoint detection only task. If both model order selection and changepoint detection are required, the prange argument should be provided as a list. Each element in this list must specify the range for a corresponding model order parameter, and the length of the list object of prange must match the number of order parameters to be estimated.

popSize

An integer represents the number of individuals/chromosomes in each popula-

pcrossover

The probability that the crossover operator will apply to the two selected parents' chromosomes to produce the offspring. The typical value is close to 1, with the

default setting in this package being 0.95.

pmutation The probability that the mutation operator applies on one individual chromo-

some. Similar to the natural mutation process, new genetic information is introduced to the offspring chromosome with a relatively small probability (close to

0), with a default value of 0.3.

pchangepoint The probability that a changepoint has occurred with a default value of 0.01.

User could change this probability based on domain knowledge and the time series length. This probability is used during population initialization and in the creation of new chromosomes by the mutation operator. By default, the mutation

operator function generates a new individual as the mutated offspring.

minDist The minimum length between two adjacent changepoints. Default value equals

The maximum number of changepoints allowed in the time series data corremmax

> sponds to the maximum possible length of  $\tau$ . For a time series of length 1000 and we only want to detect the changepoint (option="cp"), the default value is 499. The suggested value should be based on the length of the time series. For instance, if a time series has length N, the recommended mmax should be N/2-1. It is suggested to add the number of model hyperparameters if both changepoint detection and model order selection tasks are of-interested simulta-

neously (option="both").

The maximum possible length of the chromosome representation. For a time se-1max

> ries of length 1000 and we only want to detect the changepoint (option="cp"), the default value is 501. The suggested value should be based on the length of the time series. For instance, if a time series has length N, the recommended 1max should be 2 + N/2 - 1. It is suggested to add the number of model hyperparameters if both changepoint detection and model order selection tasks are

of-interested simultaneously (option="both").

The maximum number of generations the GA can run before the search is forcibly maxgen

terminated.

maxconv If the overall best fitted value doesn't change after maxconv consecutive migra-

tions, the GA algorithm stops.

option A character string controls the optimization task. "cp" indicates the task is

changepoint detection only. "both" indicates the task will include both change-

point detection and model order selection.

A logical value with either TRUE or FALSE, indicating whether to print out summonitoring

marized results (current best fitness function value and its corresponding \$C\$)

for each generation from the GA.

parallel A logical value with either TRUE or FALSE, indicating whether to use multiple

cores for parallel computation of the fitness function values for individuals after

population initialization.

An integer with the default value of NULL. It represents the number of cores

used in parallel computing. The value of nCore must be less than the number of

physical cores available.

An numerical value with the default value of 1e-05. The tolerance level that

helps evaluate whether the two iterations have the same fitness value, which

aids in determining GA termination.

nCore

tol

seed

An integer with the default value of NULL. An single integer allows function produce reproducible results.

popInitialize

A function or sourced function name character string. It should be designed for initializing a population. The default population initialization is random initialization with some imposed constraints. See random\_population for example. The function returned object is a matrix, pop. The users can specified their own population function. It could also be a matrix object, which contain the user specified chromosome. By default, each column represents one individual chromosome. See random\_population for details.

suggestions

A list object. Default value is NULL. Each element includes better or more reasonable guessed changepoints locations, which will resulting in one chromosome. If the number of provided suggestions equals to popSize, all the suggestions will be used as population. If the number of provided suggestions is less than popSize, the function from popInitialize will generate the remaining individual chromosomes. The number of provided suggestions cannot be greater than popSize. Having better suggestions can help GA converges faster.

selection

A function or sourced function name character string. This GA operator can help select mom and dad from current generation population, where dad is set to have better fit (smaller fitness function values). The default for selection uses the linear rank selection method. See <a href="mailto:selection\_linearrank">selection\_linearrank</a> for example. The function returned object is a list contain the chromosomes for mom and dad.

crossover

A function or sourced function name character string. This GA operator can apply crossover to the chosen parents to produce child for next generation with specified probability. The default for crossover uses the uniform crossover method. See uniformcrossover for details in the default crossover operator. The function returned object is a vector contain the chromosomes for child.

mutation

A function or sourced function name character string. This GA operator can apply mutation to the produced child with the specified probability pmutation. See mutation for details in the default mutation operator. The function returned object is a vector contain child chromosome representation.

. . .

additional arguments that will be passed to the fitness function.

#### **Details**

For any pre-specified time series model with a specified set of changepoint locations, model fit is evaluated using a fitness function  $Q(\theta)$ , where  $\theta=(s,\tau,\beta)'$  denotes the full parameter vector. Here, s denotes the set of model hyperparameters, potentially including the AR or MA orders, the degree of ARIMA differencing, or the periodic AR order for PAR models. The vector  $\tau=\{\tau_1,\ldots,\tau_m\}$  specifies the changepoint locations, with the number of changepoints m inferred as part of the estimation. Each individual chromosome representation is specified as a vector,

$$C = (m, \boldsymbol{s}, \boldsymbol{\tau}, N+1)',$$

where m represents the number of changepoints and is also equivalent to the length of vector  $\tau$  containing all the changepoint locations. s contains the integer-valued parameter for time series model structure specification, such as AR, MA, or PAR orders. If no model order selection is desired, then s is omitted and the GA detects changepoints only. The changepoint locations in  $\tau$ 

are encoded as interger values between 2 and N, allowing the length of  $\tau$  to vary dynamically with m. The value N+1 is appended at the end of C to serve as a delimiter marking the boundary of the chromosome.

## Value

Return an object class cptga-class. See cptga-class for a more detailed description.

## **Examples**

```
N <- 1000
XMatT <- matrix(1, nrow = N, ncol = 1)</pre>
Xt <- ts.sim(</pre>
 beta = 0.5, XMat = XMatT, sigma = 1, phi = 0.5, theta = NULL,
 Delta = c(2, -2), CpLoc = c(250, 750), seed = 1234
)
## Multiple changepoint detection without model order selection
# without suggestions
GA.res <- cptga(ObjFunc = ARIMA.BIC, N = N, XMat = XMatT, Xt = Xt)
summary(GA.res)
plot(GA.res, data = Xt)
# with suggestions
suggestions <- list(NULL, 250, c(250, 500), c(250, 625), c(250, 500, 750))
GA.res <- cptga(ObjFunc = ARIMA.BIC, N = N, suggestions = suggestions, XMat = XMatT, Xt = Xt)
summary(GA.res)
plot(GA.res, data = Xt)
## Multiple changepoint detection with model order selection
prange <- list(ar = c(0, 3), ma = c(0, 3))
# without suggestions
GA.res <- cptga(</pre>
  ObjFunc = ARIMA.BIC.Order, N = N, prange = prange,
  option = "both", XMat = XMatT, Xt = Xt
summary(GA.res)
plot(GA.res, data = Xt)
# with suggestions
suggestions <- list(NULL, 250, c(250, 500), c(250, 625), c(250, 500, 750))
GA.res <- cptga(</pre>
  ObjFunc = ARIMA.BIC.Order, N = N, prange = prange,
  suggestions = suggestions, option = "both", XMat = XMatT, Xt = Xt
summary(GA.res)
plot(GA.res, data = Xt)
```

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cptga-class

S4 Class Definition for 'cptga'

## **Description**

S4 Class for Genetic Algorithm-Based Changepoint Detection

# Usage

```
## S4 method for signature 'cptga'
summary(object, ...)
```

# Arguments

object An object of class cptga.

... Additional arguments (ignored).

## **Details**

An object of class cptga stores results and configuration settings for changepoint detection using a Genetic Algorithm (GA), optionally with simultaneous model order selection. This class records GA control parameters, intermediate population structures, and the optimal solution found.

#### Value

An object of class cptga.

# Slots

call The matched call that created the object.

N The sample size of the time series.

prange A list object. Default is NULL. If specified, it contains the ranges for each model order parameter (integers). Required when option = "both" is used for joint changepoint and model selection.

popSize An integer representing the number of individuals in each GA population.

pcrossover The probability that the crossover operator is applied to two chromosomes.

pmutation The probability that the mutation operator is applied to a chromosome.

pchangepoint The prior probability that a changepoint has occurred at each location.

minDist The minimum allowed distance between two adjacent changepoints.

mmax The maximum possible number of changepoints. Typically set based on time series length and option.

lmax The maximum length of the chromosome. Typically set based on time series length and option.

maxgen The maximum number of generations the GA is allowed to run.

maxconv If the optimal fitness value does not improve over this many generations, GA stops.

option A character string: either "cp" for changepoint detection only, or "both" for changepoint detection and model order selection.

monitoring Logical. If TRUE, prints intermediate GA progress.

parallel Logical. If TRUE, enables parallel computation for fitness evaluation.

nCore Integer or NULL. Number of cores used for parallel computation when parallel = TRUE.

tol Numeric. Tolerance for determining GA convergence. Default is 1e-5.

seed An integer or NULL. Random seed for reproducibility.

suggestions A list or NULL. Each element provides suggested changepoint locations to guide initial population design and potentially accelerate convergence.

population A matrix where each row represents an individual chromosome in the current popula-

fitness A numeric vector containing the fitness values of individuals in the current generation.

overbestchrom A vector representing the best chromosome found over all generations.

overbestfit A numeric scalar. The best (smallest) fitness value achieved.

bestfit A numeric vector recording the best fitness value in each generation.

count A numeric value indicating the number of generations the GA actually ran.

convg A numeric vector representing convergence information. A value of 0 indicates the algorithm successful completion. A value of 1 indicates the total number of generations exceeds the pre-specified maxgen limit.

#### See Also

cptga, cptga-class, random\_population, selection\_linearrank, uniformcrossover, mutation.

cptgaisl

Island model based genetic algorithm

## **Description**

Perform the modified island-based genetic algorithm (IslandGA) for multiple changepoint detection. Minimization of an objective function using genetic algorithm (GA). The algorithm can be run sequentially or in explicit parallelisation.

# Usage

```
cptgaisl(
   ObjFunc,
   N,
   prange = NULL,
   popSize = 200,
   numIslands = 5,
   pcrossover = 0.95,
```

```
pmutation = 0.3,
 pchangepoint = 0.01,
 minDist = 1,
 mmax = NULL,
 1max = NULL,
 maxMig = 1000,
 maxgen = 50,
 maxconv = 100,
 option = "cp",
 monitoring = FALSE,
 parallel = FALSE,
 nCore = NULL,
  tol = 1e-05,
  seed = NULL,
  popInitialize = "random_population",
  suggestions = NULL,
  selection = "selection_linearrank",
  crossover = "uniformcrossover",
 mutation = "mutation",
)
```

## **Arguments**

**ObjFunc** 

The fitness function to be minimized. Users can specify any R or Rcpp function as the fitness function, setting the input as the potential solution to the optimization problem and returning a numerical value as the output/fitness. Depending on the user-specified chromosome representation, the optimization task can be changepoint detection only or changepoint detection plus model order selection, which can be specified via the option parameter. When option="both", the list prange must be specified to give the range of model orders.

Ν

The sample size of the time series.

prange

The default value is NULL for changepoint detection only task. If both model order selection and changepoint detection are required, the prange argument should be provided as a list. Each element in this list must specify the range for a corresponding model order parameter, and the length of the list object of prange must match the number of order parameters to be estimated.

popSize

An integer representing the total number of individuals in each generation, which equal to the number of islands multiplied by the size of each island (i.e., popSize = numIslands × Islandsize).

 ${\tt numIslands}$ 

An integer representing the number of islands (sub-populations).

pcrossover

The probability that the crossover operator will apply to the two selected parents' chromosomes to produce the offspring. The typical value is close to 1, with the default setting in this package being 0.95.

pmutation

The probability that the mutation operator applies on one individual chromosome. Similar to the natural mutation process, new genetic information is introduced to the offspring chromosome with a relatively small probability (close to 0), with a default value of 0.3.

pchangepoint The pr

The probability that a changepoint has occurred. User could change this probability based on domain knowledge and the time series length. This probability is used during population initialization and in the creation of new chromosomes by the mutation operator. By default, the mutation operator function generates a new individual as the mutated offspring.

minDist

The minimum length between two adjacent changepoints. Default value equals to one.

mmax

The maximum number of changepoints allowed in the time series data corresponds to the maximum possible length of  $\tau$ . For a time series of length 1000 and we only want to detect the changepoint (option="cp"), the default value is 499. The suggested value should be based on the length of the time series. For instance, if a time series has length N, the recommended mmax should be N/2-1. It is suggested to add the number of model hyperparameters if both changepoint detection and model order selection tasks are of-interested simultaneously (option="both").

1max

The maximum possible length of the chromosome representation. For a time series of length 1000 and we only want to detect the changepoint (option="cp"), the default value is 501. The suggested value should be based on the length of the time series. For instance, if a time series has length N, the recommended lmax should be 2+N/2-1. It is suggested to add the number of model hyperparameters if both changepoint detection and model order selection tasks are of-interested simultaneously (option="both").

maxMig

An integer indicates the maximum number of migrations. After conducting maxMig migrations, the island model GA stops.

maxgen

An integer indicates the maximum number of generations that each island (sub-population) undergoes before migration. It also determines the requency of migration. The migration will occur after maxgen generations for each island (sub-population).

maxconv

An integer value is also used for algorithm termination. If the overall bestfitted value remains unchanged after maxconv consecutive migrations, the island model GA will terminate.

option

A character string controls the optimization task. "cp" indicates the task is changepoint detection only. "both" indicates the task will include both changepoint detection and model order selection.

monitoring

A logical value with either TRUE or FALSE, indicating whether to print out summarized results (current best fitness function value and its corresponding \$C\$) for each generation from the GA.

parallel

A logical value with TRUE or FALSE, indicating whether to use multiple cores for parallel computation. Different from the basic GA, in this approach, each island evolves independently. New population generation—including parent selection, crossover, and mutation—is processed independently and in parallel for each island, further saving computation time. Once the new population generation is complete, the migration operator is performed sequentially.

nCore

An integer indicates the number of cores utilized in parallel computing. For the island model GA, the number of cores used in parallel is set to the numIslands for convenience.

An numerical value with the default value of 1e-05. The tolerance level that

helps evaluate whether the two iterations have the same fitness value, which

aids in determining GA termination.

seed An integer with the default value of NULL. An single integer allows function

produce reproducible results.

popInitialize A function or sourced function name character string. It should be designed for

initializing a population. The default population initialization is random initialization with some imposed constraints. See random\_population for example. The function returned object is a matrix, pop. The users can specified their own population function. It could also be a matrix object, which contain the user specified chromosome. By default, each column represents one individual

chromosome. See random\_population for details.

suggestions A list object. Default value is NULL. Each element includes better or more rea-

sonable guessed changepoints locations, which will resulting in one chromosome. If the number of provided suggestions equals to popSize, all the suggestions will be used as population. If the number of provided suggestions is less than popSize, the function from popInitialize will generate the remaining individual chromosomes. The number of provided suggestions cannot be greater

than popSize. Having better suggestions can help GA converges faster.

selection A function or sourced function name character string. This GA operator can

help select mom and dad from current generation population, where dad is set to have better fit (smaller fitness function values). The default for selection uses the linear rank selection method. See selection\_linearrank for example.

The function returned object is a list contain the chromosomes for mom and dad.

A function or sourced function name character string. This GA operator can apply crossover to the chosen parents to produce child for next generation with specified probability. The default for crossover uses the uniform crossover method.

See uniformcrossover for details in the default crossover operator. The func-

tion returned object is a vector contain the chromosomes for child.

mutation A function or sourced function name character string. This GA operator can

apply mutation to the produced child with the specified probability pmutation. See mutation for details in the default mutation operator. The function returned

object is a vector contain child chromosome representation.

... additional arguments that will be passed to the fitness function.

#### **Details**

For any pre-specified time series model with a specified set of changepoint locations, model fit is evaluated using a fitness function  $Q(\theta)$ , where  $\theta=(s,\tau,\beta)'$  denotes the full parameter vector. Here, s denotes the set of model hyperparameters, potentially including the AR or MA orders, the degree of ARIMA differencing, or the periodic AR order for PAR models. The vector  $\tau=\{\tau_1,\ldots,\tau_m\}$  specifies the changepoint locations, with the number of changepoints m inferred as part of the estimation. Each individual chromosome representation is specified as a vector,

$$C = (m, \boldsymbol{s}, \boldsymbol{\tau}, N+1)',$$

where m represents the number of changepoints and is also equivalent to the length of vector  $\tau$  containing all the changepoint locations. s contains the integer-valued parameter for time series

model structure specification, such as AR, MA, or PAR orders. If no model order selection is desired, then s is omitted and the GA detects changepoints only. The changepoint locations in  $\tau$  are encoded as interger values between 2 and N, allowing the length of  $\tau$  to vary dynamically with m. The value N+1 is appended at the end of C to serve as a delimiter marking the boundary of the chromosome.

#### Value

Return an object class cptgaisl-class. See cptgaisl-class for a more detailed description.

# **Examples**

```
N <- 1000
XMatT \leftarrow matrix(1, nrow = N, ncol = 1)
Xt <- ts.sim(</pre>
 beta = 0.5, XMat = XMatT, sigma = 1, phi = 0.5, theta = NULL,
  Delta = c(2, -2), CpLoc = c(250, 750), seed = 1234
## Multiple changepoint detection without model order selection
# without suggestions
GAISL.res <- cptgaisl(ObjFunc = ARIMA.BIC, N = N, XMat = XMatT, Xt = Xt)
summary(GAISL.res)
plot(GAISL.res, data = Xt)
# with suggestions
suggestions <- list(NULL, 250, c(250, 500), c(250, 625), c(250, 500, 750))
GAISL.res <- cptgaisl(ObjFunc = ARIMA.BIC, N = N, suggestions = suggestions, XMat = XMatT, Xt = Xt)
summary(GAISL.res)
plot(GAISL.res, data = Xt)
## Multiple changepoint detection with model order selection
prange <- list(ar = c(0, 3), ma = c(0, 3))
# without suggestions
GAISL.res <- cptgaisl(</pre>
  ObjFunc = ARIMA.BIC.Order, N = N, prange = prange,
  option = "both", XMat = XMatT, Xt = Xt
)
summary(GAISL.res)
plot(GAISL.res, data = Xt)
# with suggestions
suggestions <- list(NULL, 250, c(250, 500), c(250, 625), c(250, 500, 750))
GAISL.res <- cptgaisl(</pre>
  ObjFunc = ARIMA.BIC.Order, N = N, prange = prange,
  suggestions = suggestions, option = "both", XMat = XMatT, Xt = Xt
)
```

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```
summary(GAISL.res)
plot(GAISL.res, data = Xt)
```

cptgaisl-class

S4 Class Definition for 'cptgaisl'

# **Description**

S4 Class for Island Model Genetic Algorithm-Based Changepoint Detection

# Usage

```
## S4 method for signature 'cptgaisl'
summary(object, ...)
```

# Arguments

object An object of class cptgaisl.
... Additional arguments (ignored).

#### **Details**

This class stores results and settings for the island model genetic algorithm ('cptgaisl') used in multiple changepoint detection and optional model order selection.

# Value

An object of class cptgaisl

#### **Slots**

call The matched call that created the object.

N The sample size of the time series.

prange A list or NULL. Ranges for each model order parameter when option = "both".

popSize Integer. It represents the total number of individuals in each generation, which equal to the number of islands multiplied by the size of each island (i.e., popSize = numIslands × Islandsize).

numIslands Integer. The number of islands (sub-populations).

Islandsize Numerical value. The number of individuals in each island.

pcrossover Probability of crossover operation.

pmutation Probability of mutation operation.

pchangepoint Prior probability of changepoint occurrence.

minDist Minimum distance between adjacent changepoints.

mmax Maximum number of changepoints allowed.

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1max Maximum length of chromosome.

maxMig Maximum number of migrations allowed.

maxgen Maximum number of generations per island before migration.

maxconv Number of migrations with no improvement before stopping.

option Either "cp" or "both".

monitoring Logical. If TRUE, prints intermediate output.

parallel Logical. Whether parallel computation is used.

nCore Integer or NULL. Number of cores for parallelization.

tol Tolerance threshold for fitness improvement.

seed Integer or NULL. Seed for reproducibility.

suggestions A list or NULL. Suggested changepoint configurations.

Island A 3D array storing all individual chromosomes in current generation across islands. Dimensions are lmax × Islandsize × numIslands, representing chromosome length, individuals per island, and number of islands, respectively.

IslandFit A matrix of fitness values in current generation with dimensions Islandsize × numIslands, where each column corresponds to one island's population.

overbestchrom A vector. The best chromosome ever found.

overbestfit Numeric. The best fitness score obtained.

bestfit Numeric vector recording best fitness per migration.

countMig Integer vector tracking number of migrations.

count Integer vector tracking total generations.

convg Integer vector for convergence diagnostics.

#### See Also

cptgaisl, cptgaisl-class, random\_population, selection\_linearrank, uniformcrossover, mutation.

mutation

The default mutation operator in genetic algorithm

## **Description**

In a certain probability, the mutation genetic operator can be applied to generate a new child. By default, the new child selection can be down by the similar individual selection method in population initialization, selectTau.

# Usage

```
mutation(child, prange = NULL, minDist, pchangepoint, lmax, mmax, N)
```

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## Arguments

child The child chromosome resulting from the crossover genetic operator.

prange Default is NULL for only changepoint detection. If prange is specified as a list

object, which contains the range of each model order parameters for order selection (integers). The number of order parameters must be equal to the length

of prange.

minDist The required minimum distance between two adjacent changepoints.

pchangepoint The probability of changepoints for every time series.

1max The user specified maximum number of changepoints, by default, as N/2 - 1.

mmax The user specified maximum length of individual chromosome, by default, as

2+N/2+1.

N The sample size of the time series.

#### **Details**

A function can apply mutation to the produced child with the specified probability pmutation in cptga and cptgaisl. If order selection is not requested (option = "cp" in cptga and cptgaisl), the default mutation operator function uses selectTau to select a completely new individual with a new chromosome as the mutated child. For details, see selectTau. If order selection is needed (option = "both" in cptga and cptgaisl), we first decide whether to keep the produced child's model order with a probability of 0.5. If the child's model order is retained, the selectTau function is used to select a completely new individual with a new chromosome as the mutated child. If a new model order is selected from the candidate model order set, there is a 0.5 probability to either select a completely new individual with new changepoint locations or retain the original child's changepoint locations for the mutated child. Note that the current model orders in the child's chromosome are excluded from the set to avoid redundant objective function evaluation. Finally, the function returns a vector containing the modified chromosomes for mutated child.

# Value

The resulting child chromosome representation.

plot.cptga Plot Time Series with Detected Changepoints from a 'cptga' Object

# **Description**

This function visualizes a univariate time series along with the changepoints identified by a basic genetic algorithm, as represented by a 'cptga' object. Vertical dashed lines mark changepoint locations, and segment means are shown as horizontal dashed lines. The optimal fitness value and changepoint locations are displayed as margin text.

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# Usage

```
## S3 method for class 'cptga'
plot(
    x,
    data,
    main = NULL,
    XTickLab = NULL,
    XTickPos = NULL,
    XAxisLab = "Time",
    YAxisLab = "Data",
    cex.lab = 1.3,
    cex.axis = 1.3,
    cex.main = 1.3,
    lwd = 2,
    ...
)
```

## **Arguments**

X	An object of class cptgaisl, typically returned by a basic genetic algorithm based changepoint detection procedure.
data	A numeric vector representing the observed univariate time series.
main	Optional main title for the plot.
XTickLab	Optional vector (e.g., numeric or date) for custom x-axis labels. Must be the same length as data.
XTickPos	Optional vector specifying which elements of XTickLab to show as ticks.
XAxisLab	Optional label for the x-axis. Default is "Time".
YAxisLab	Optional label for the y-axis. Default is "Data".
cex.lab	Text size for axis labels and margin text. Default is 1.3.
cex.axis	Text size for axis tick labels. Default is 1.3.
cex.main	Text size for the main title. Default is 1.3.
lwd	Line width for vertical and horizontal dashed lines. Default is 2.
	Additional graphical parameters passed to plot().

# Details

If XTickLab is supplied and matches the length of data, it is used for the x-axis; otherwise, the default sequence 1:length(data) is used.

If the genetic algorithm was run with option = "both", the function skips hyperparameters in the chromosome when extracting changepoint positions.

The plot displays vertical dashed lines at changepoint locations and horizontal dashed lines for the mean of each segment. Fitness and changepoint summaries are shown above the plot.

# Value

This function is called for its side effects and returns NULL invisibly.

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# See Also

```
cptga, summary, plot.cptga
```

plot.cptgaisl

Plot Time Series with Detected Changepoints from a 'cptgaisl' Object

# Description

This function visualizes a univariate time series along with the changepoints identified by a island model genetic algorithm, as represented by a 'cptgaisl' object. Vertical dashed lines mark changepoint locations, and segment means are shown as horizontal dashed lines. The optimal fitness value and changepoint locations are displayed as margin text.

# Usage

```
## $3 method for class 'cptgaisl'
plot(
    X,
    data,
    main = NULL,
    XTickLab = NULL,
    XTickPos = NULL,
    XAxisLab = "Time",
    YAxisLab = "Data",
    cex.lab = 1.3,
    cex.axis = 1.3,
    cex.main = 1.3,
    lwd = 2,
    ...
)
```

# Arguments

X	An object of class cptgaisl, typically returned by an island model genetic algorithm based changepoint detection procedure.
data	A numeric vector representing the observed univariate time series.
main	Optional main title for the plot.
XTickLab	Optional vector (e.g., numeric or date) for custom $x$ -axis labels. Must be the same length as data.
XTickPos	Optional vector specifying which elements of XTickLab to show as ticks.
XAxisLab	Optional label for the x-axis. Default is "Time".
YAxisLab	Optional label for the y-axis. Default is "Data".
cex.lab	Text size for axis labels and margin text. Default is 1.3.
cex.axis	Text size for axis tick labels. Default is 1.3.

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cex.main	Text size for the main title. Default is 1.3.
lwd	Line width for vertical and horizontal dashed lines. Default is 2.
	Additional graphical parameters passed to plot().

#### **Details**

If XTickLab is supplied and matches the length of data, it is used for the x-axis; otherwise, the default sequence 1:length(data) is used.

If the genetic algorithm was run with option = "both", the function skips hyperparameters in the chromosome when extracting changepoint positions.

The plot displays vertical dashed lines at changepoint locations and horizontal dashed lines for the mean of each segment. Fitness and changepoint summaries are shown above the plot.

#### Value

This function is called for its side effects and returns NULL invisibly.

#### See Also

```
summary, print.summary.cptgaisl
```

```
print.summary.cptga Print Summary for a 'cptga' Object
```

# **Description**

Displays key information about the settings and results from a changepoint detection procedure using the Genetic Algorithm (GA) stored in a 'cptga' object. This includes the algorithm configuration, population settings, optimization mode, and final solution such as the number and location of changepoints and model parameters (if applicable).

#### **Usage**

```
## S3 method for class 'summary.cptga'
print(x, digits = getOption("digits"), max_display = 5, ...)
```

# Arguments

х	An object of class cptga, typically produced by a GA-based changepoint detection routine.
digits	$Number of digits to print for probabilities and fitness. Default taken from {\tt getOption("digits")}.$
max_display	Maximum number of suggested solutions to display if suggestions are provided.
	Additional arguments (currently not used).

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#### **Details**

When the GA is run in option = "cp" mode, only changepoint locations are shown. If option = "both", the output includes the selected model hyperparameters along with changepoint locations.

The function uses plain text output to print a formatted summary to the console. If x@suggestions is provided, only up to max\_display suggestions will be shown.

#### Value

Invisibly returns NULL. Called for its side effect of printing to the console.

#### See Also

```
cptga, summary, plot.cptga
```

```
print.summary.cptgaisl
```

Print Summary for a 'cptgaisl' Object

#### **Description**

Displays key information about the settings and results from a changepoint detection procedure using the Island model Genetic Algorithm (IMGA) stored in a 'cptgaisl' object. This includes the algorithm configuration, population settings, optimization mode, and final solution such as the number and location of changepoints and model parameters (if applicable).

# Usage

```
## S3 method for class 'summary.cptgaisl'
print(x, digits = getOption("digits"), max_display = 5, ...)
```

## Arguments

X	An object of class cptgais1, typically produced by a GA-based changepoint detection routine.
digits	$Number of \ digits \ to \ print \ for \ probabilities \ and \ fitness. \ Default \ taken \ from \ getOption("digits").$
max_display	Maximum number of suggested solutions to display if suggestions are provided.
	Additional arguments (currently not used).

#### **Details**

When the GA is run in option = "cp" mode, only changepoint locations are shown. If option = "both", the output includes the selected model hyperparameters along with changepoint locations.

The function uses plain text output to print a formatted summary to the console. If x@suggestions is provided, only up to max\_display suggestions will be shown.

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#### Value

Invisibly returns NULL. Called for its side effect of printing to the console.

#### See Also

```
cptgaisl, summary, plot.cptgaisl
```

random\_population Random population initialization

## **Description**

Randomly generate the individuals' chromosomes (changepoint confirgurations) to construct the first generation population.

# Usage

random\_population(popSize, prange, N, minDist, pchangepoint, mmax, lmax)

# Arguments

popSize	An integer represents the number of individual in each population for GA (or subpopulation for IslandGA).
prange	Default is NULL for only changepoint detection. If prange is specified as a list object, which contains the range of each model order parameters for order selection (integers). The number of order parameters must be equal to the length of prange.
	TTILL ALCOHOL:

N The length of time series.

minDist The minimum length between two adjacent changepoints.

pchangepoint Same as pchangepoint from cptga or cptgaisl, the probability that a change-

point has occurred.

mmax The maximum possible number of changepoints in the data set.

1max The maximum possible length of the chromosome representation.

# **Details**

Each population can be stored in a matrix with lmax rows and popSize columns, where each column represents an individual chromosome in the format of

$$C = (m, \boldsymbol{s}, \boldsymbol{\tau}, N+1)',$$

in cptga or cptgaisl. This function can randomly initialize the population matrix with some imposed constraints, such as ensuring the number of time points between two adjacent changepoints is greater than or equal to minDist. This prevents unrealistic scenario of two changepoints being too close to each other and helps reduce the total number of admissible solutions in the search space. Users can adjust the level of searching space reduction by setting an appropriate value for minDist.

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During population initialization, each changepoint location in  $\tau$  can be selected sequentially. With a specified probability pchangepoint denoting the probability of a time point being selected as a changepoint, the first changepoint  $\tau_1$  is randomly picked between t=1+minDist and t=N. Then  $\tau_2$  is randomly selected from a smaller range between  $t=\tau_1+minDist$  and t=N. The process is continued until the last admissible changepoint t=N-minDist is exceeded, and the number of changepoints m is obtained automatically. For added flexibility, users can specify their own population initialization function. The default population initialization uses selectTau to select the chromosome for the first generation population.

## Value

A matrix that contains each individual's chromosome.

## Description

The genetic algorithm require to select a pair of chromosomes, representing dad and mom, for the crossover operator to produce offspring (individual for next generation). The parents chromosomes are randomly selected from the initialized population by a linear ranking method according to each individual's fittness in the input argument popFit. By default, the dad has better fit/smaller fitness function value/larger rank than mom.

## Usage

selection\_linearrank(pop, popFit)

#### **Arguments**

pop A matrix contains the chromosomes for all individuals. The number of rows is

equal to 1max and the number of columns is equal to the popSize.

popFit A vector contains the objective function value (population fit) being associated

to each individual chromosome from above.

#### Value

A list contains the chromosomes for dad and mom.

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lect <sup>-</sup>	

Randomly select the chromosome

# Description

Randomly select the changepoint configuration for population initialization. The selected changepoint configuration represents a changepoint chromosome. The first element of the chromosome represent the number of changepoints and the last non-zero element always equal to the length of time series + 1.

## Usage

```
selectTau(N, prange, minDist, pchangepoint, mmax, lmax)
```

## **Arguments**

N The length of time series.

prange A list object containing the possible range for other pre-defined model parame-

ters, i.e. AR/MA order of ARMA models.

minDist The minimum length between two adjacent changepoints.

pchangepoint Same as Pchangepoint, the probability that a changepoint has occurred.

mmax The maximum possible number of changepoints in the data set.

1max The maximum possible length of the chromosome representation.

#### Value

A single changepoint configuration format as above.

ts.sim

Time series simulation with changepoint effects

# **Description**

This is a function to simulate time series with changepoint effects. See details below.

## Usage

```
ts.sim(
  beta,
  XMat,
  sigma,
  phi = NULL,
  theta = NULL,
  Cploc = NULL,
  seed = NULL
)
```

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#### **Arguments**

b	eta	A parameter vector contains other mean function parameters without change- point parameters.
XI	Mat	The covairates for time series mean function without changepoint indicators.
s	igma	The standard deviation for time series residuals $\epsilon_t$ .
р	hi	A vector for the autoregressive (AR) parameters for AR part.
t	heta	A vector for the moving average (MA) parameters for MA part.
D	elta	The parameter vector contains the changepoint parameters for time series mean function.
C	pLoc	A vector contains the changepoint locations range from $1 \le \tau \le T_s$ .
S	eed	The random seed for simulation reproducibility.

#### **Details**

The simulated time series  $Z_t, t = 1, \dots, T_s$  is from a class of models,

$$Z_t = \mu_t + e_t$$
.

- Time series observations are IID  $\mu_t$  is a constant and  $e_t$ 's are independent and identically distributed as  $N(0,\sigma)$ .
- ARMA(p,q) model with constant mean  $\mu_t$  is a constant, and  $e_t$  follows an ARMA(p,q) process.
- ARMA(p,q) model with seasonality μ<sub>t</sub> is not a constant,

$$\mu_t = ASin(\frac{2\pi t}{S}) + BSin(\frac{2\pi t}{S}),$$

and  $e_t$  follows an ARMA(p,q) process.

 ARMA(p,q) model with seasonality and trend μ<sub>t</sub> is not a constant,

$$\mu_t = ASin(\frac{2\pi t}{S}) + BSin(\frac{2\pi t}{S}) + \alpha t,$$

and  $e_t$  follows an ARMA(p,q) process. The changepoint effects could be introduced through the  $\mu_t$  as

$$\mu_t = \Delta_1 I_{t > \tau_1} + \ldots + \Delta_m I_{t > \tau_m},$$

where  $1 \leq \tau_1 < \ldots < \tau_m \leq T_s$  are the changepoint locations and  $\Delta_1, \ldots, \Delta_m$  are the changepoint parameter that need to be estimated.

## Value

The simulated time series with attributes:

Z The simulated time series.

Attributes • DesignX The covariates include all changepoint indicators.

- mu A vector includes the mean values for simulated time series sequences.
- theta The true parameter vector (including changepoint effects).

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- CpEff The true changepoint magnitudes.
- CpLoc The true changepoint locations where we introduce the mean changing effects.
- arEff A vector givies the AR coefficients.
- maEff A vector givies the MA coefficients.
- seed The random seed used for this simulation.

# **Examples**

```
##### M1: Time series observations are IID
Ts <- 1000
betaT <- c(0.5) # intercept
XMatT <- matrix(1, nrow = Ts, ncol = 1)</pre>
colnames(XMatT) <- "intercept"</pre>
sigmaT <- 1
DeltaT <- c(2, -2)
Cp.prop <- c(1 / 4, 3 / 4)
CpLocT <- floor(Ts * Cp.prop)</pre>
myts <- ts.sim(</pre>
  beta = betaT, XMat = XMatT, sigma = sigmaT,
  Delta = DeltaT, CpLoc = CpLocT, seed = 1234
)
##### M2: ARMA(2,1) model with constant mean
Ts <- 1000
betaT <- c(0.5) # intercept
XMatT <- matrix(1, nrow = Ts, ncol = 1)</pre>
colnames(XMatT) <- "intercept"</pre>
sigmaT <- 1
phiT <- c(0.5, -0.5)
thetaT <- c(0.8)
DeltaT <- c(2, -2)
Cp.prop <- c(1 / 4, 3 / 4)
CpLocT <- floor(Ts * Cp.prop)</pre>
myts <- ts.sim(</pre>
  beta = betaT, XMat = XMatT, sigma = sigmaT,
  phi = phiT, theta = thetaT, Delta = DeltaT, CpLoc = CpLocT, seed = 1234
##### M3: ARMA(2,1) model with seasonality
Ts <- 1000
betaT <- c(0.5, -0.5, 0.3) # intercept, B, D
period <- 30
XMatT <- cbind(rep(1, Ts), cos(2 * pi * (1:Ts) / period), sin(2 * pi * (1:Ts) / period))
colnames(XMatT) <- c("intercept", "Bvalue", "DValue")</pre>
sigmaT <- 1
phiT <- c(0.5, -0.5)
thetaT <- c(0.8)
DeltaT \leftarrow c(2, -2)
Cp.prop <- c(1 / 4, 3 / 4)
```

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```
CpLocT <- floor(Ts * Cp.prop)</pre>
myts <- ts.sim(</pre>
  beta = betaT, XMat = XMatT, sigma = sigmaT,
  phi = phiT, theta = thetaT, Delta = DeltaT, CpLoc = CpLocT, seed = 1234
)
##### M4: ARMA(2,1) model with seasonality and trend
# scaled trend if large number of sample size
Ts <- 1000
betaT <- c(0.5, -0.5, 0.3, 0.01) # intercept, B, D, alpha
period <- 30
XMatT \leftarrow cbind(rep(1, Ts), cos(2 * pi * (1:Ts) / period), sin(2 * pi * (1:Ts) / period), 1:Ts)
colnames(XMatT) <- c("intercept", "Bvalue", "DValue", "trend")</pre>
sigmaT <- 1
phiT <- c(0.5, -0.5)
thetaT <- c(0.8)
DeltaT <- c(2, -2)
Cp.prop <- c(1 / 4, 3 / 4)
CpLocT <- floor(Ts * Cp.prop)</pre>
myts <- ts.sim(</pre>
  beta = betaT, XMat = XMatT, sigma = sigmaT,
  phi = phiT, theta = thetaT, Delta = DeltaT, CpLoc = CpLocT, seed = 1234
)
```

uniformcrossover

Uniform crossover to produce offsprings

## **Description**

In uniform crossover, typically, each bit is chosen from either parent with equal probability. Other mixing ratios are sometimes used, resulting in offspring which inherit more genetic information from one parent than the other. In a uniform crossover, we don't divide the chromosome into segments, rather we treat each gene separately. In this, we essentially flip a coin for each chromosome to decide whether or not it will be included in the off-spring. If model order selection is requested, each child's model order has the equal probability (0.5) from dad and mom.

## Usage

```
uniformcrossover(mom, dad, prange, minDist, lmax, N)
```

## **Arguments**

mom	Among two selected individuals, mom represents the selected chromosome representation with lower fitness function value.
dad	Among two selected individuals, dad represents the selected chromosome rep-

resentation with larger fitness function value.

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prange Default value is NULL for only changepoint detection. If prange is specified as

a list object, which contains the range of each model order parameters for order selection (integers). The number of order parameters must be equal to the length

of prange.

minDist The required minimum distance between two adjacent changepoints.

1max The user specified maximum number of changepoints, by default, as N/2 - 1.

N The length of time series.

# Value

The child chromosome that produced from mom and dad for next generation.

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